



# Syntactic and Dependency Parsing

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CS 421: Natural Language  
Processing

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Many slides adapted from Jurafsky and Martin  
(<https://web.stanford.edu/~jurafsky/slp3/>) and  
Ben-Gurion University's NLP course  
(<https://www.cs.bgu.ac.il/~michaluz/seminar/CKY1.pdf>).

# What is syntactic parsing?

The process of automatically recognizing sentences and assigning syntactic (grammatical) structure to them.

# Why is syntactic parsing useful?

- Lots of reasons!
  - Grammar checking
    - Sentences that can't be parsed may be grammatically incorrect (or at least hard to read)
  - Semantic analysis
  - Downstream applications
    - Question answering
    - Information extraction

What **courses** were **taught** by UIC CS assistant professors in 2019?



Subject = courses ...don't return a list of UIC CS assistant professors!

# Parsing algorithms are one of the core tools for analyzing natural language.

- Parsing algorithms automatically describe the syntactic structure of sentences in terms of **context-free grammars** (such as those discussed last week)
- This can be viewed as a **search problem**:
  - Given the set of all possible parse trees, find the correct parse tree for this sentence.

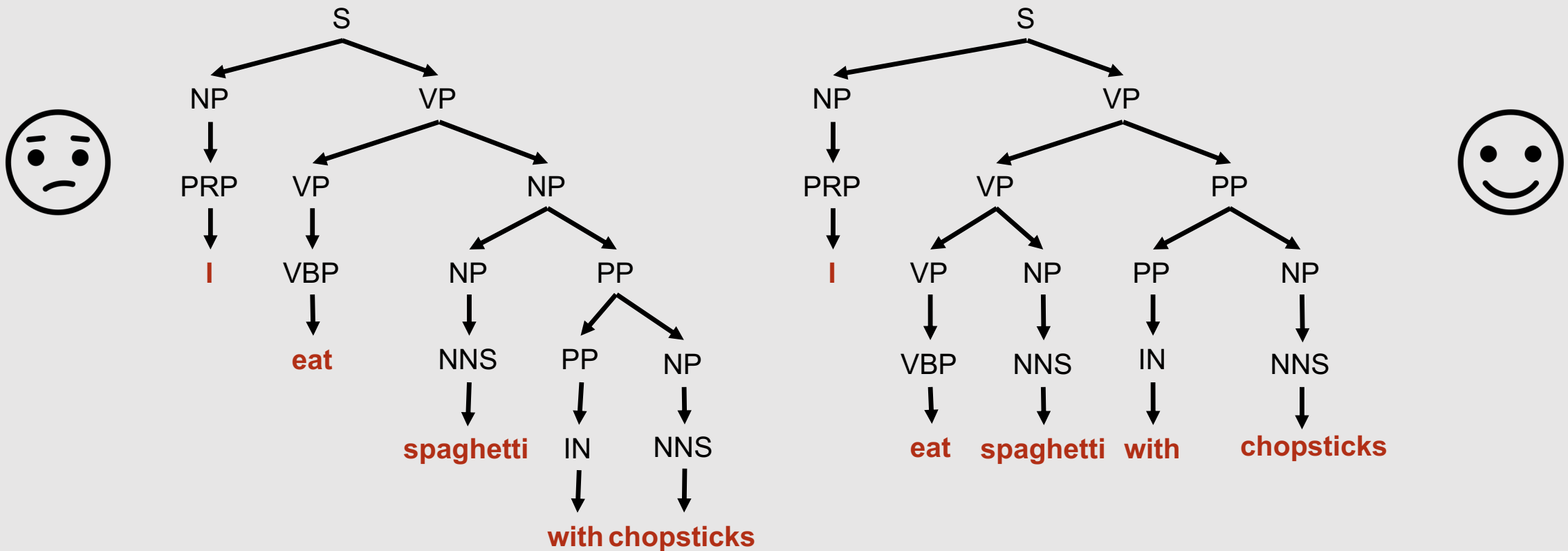


# Recognition vs. Parsing

- **Recognition:** Deciding whether a sentence belongs to the language specified by a formal grammar.
- **Parsing:** Producing a parse tree for the sentence based on that formal grammar.
- Both tasks are necessary for generating correct syntactic parses!
  - Failure to accurately recognize whether a sentence can be parsed will lead to **misparses**, which will in turn lead to additional errors in downstream applications.
- Parsing is more “difficult” (greater time complexity) than recognition

# Remember, language is ambiguous!

Input sentences may have many possible parses



**There are many ways to generate parse trees.**

### Top-Down Parsing:

- Goal-driven
- Builds parse tree from the start symbol down to the terminal nodes

### Bottom-Up Parsing:

- Data-driven
- Builds parse tree from the terminal nodes up to the start symbol

**Naïve approach:**  
Enumerate all possible  
solutions

**Dynamic programming  
approach:** Save partial  
solutions in a table, and  
use this information to  
reduce search time

**These approaches can be implemented naïvely,  
or using more advanced techniques.**



# Top-Down Parsing

- Assume that the input can be derived by the designated start symbol **S**
- Find the tops of all trees that can start with **S**
  - Look for all production rules with **S** on the left-hand side
- Find the tops of all trees that can start with those constituents
- (Repeat recursively until POS categories at bottom of tree are reached)
- Trees whose leaves fail to match all words in the input sentence can be rejected, leaving behind trees that represent successful parses

# Top-Down Parsing: Example

## Input Sentence:

Book that flight.

## Grammar:

S → NP VP  
S → Aux NP VP  
S → VP  
NP → Pronoun  
NP → Proper-Noun  
NP → Det Nominal  
Nominal → Noun  
Nominal → Nominal Noun  
Nominal → Nominal PP  
VP → Verb  
VP → Verb NP  
VP → Verb NP PP  
VP → Verb PP  
VP → VP PP  
PP → Preposition NP

## Lexicon:

Det → that | this | a  
Noun → book | flight | meal | money  
Verb → book | include | prefer  
Pronoun → I | she | me  
Proper-Noun → Houston | NWA  
Aux → does  
Preposition → from | to | on | near | through

# Top-Down Parsing: Example

Book that flight.

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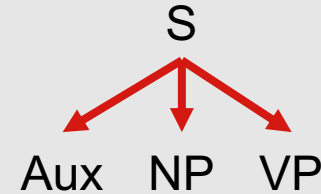
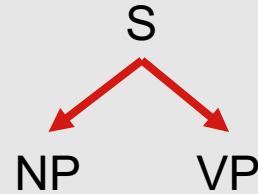
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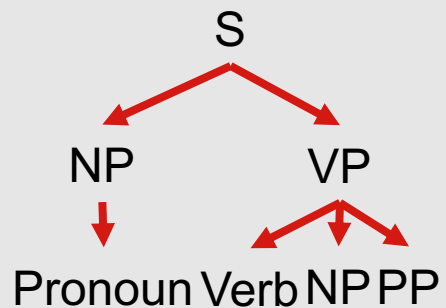
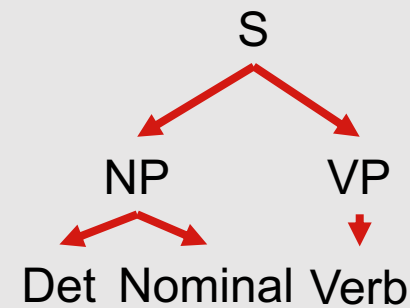
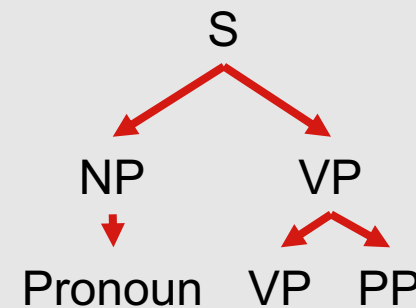
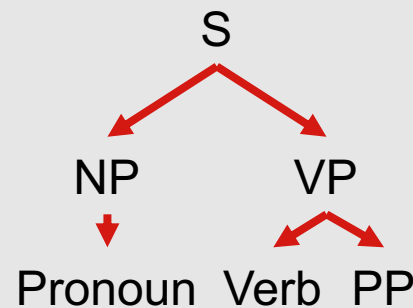
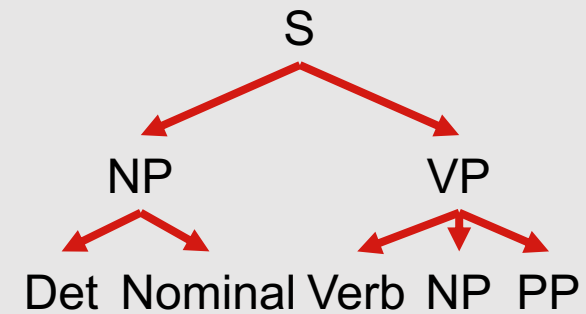
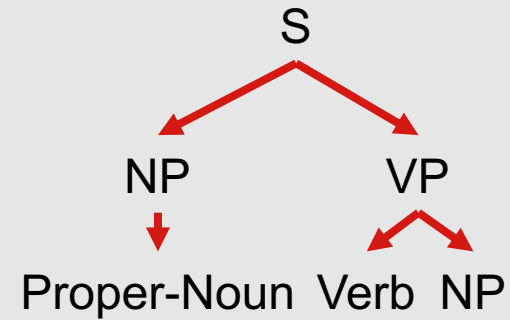
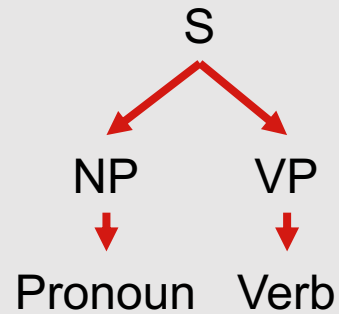
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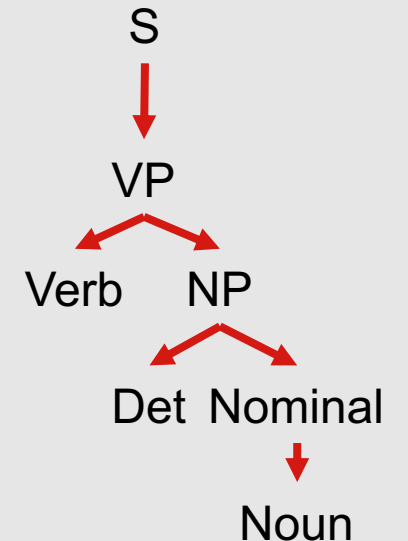
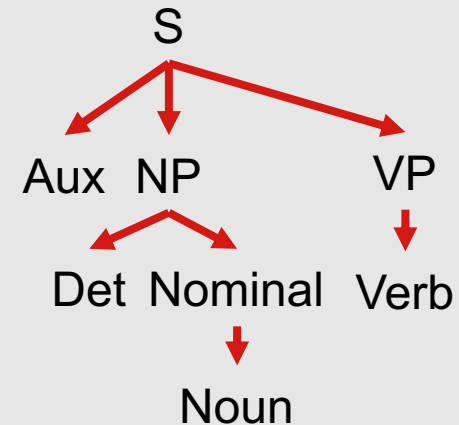
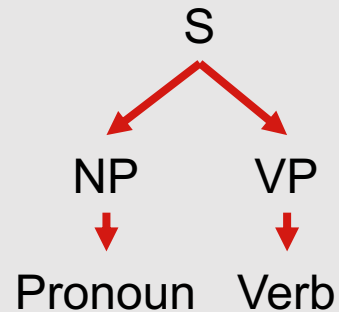


...and many more!

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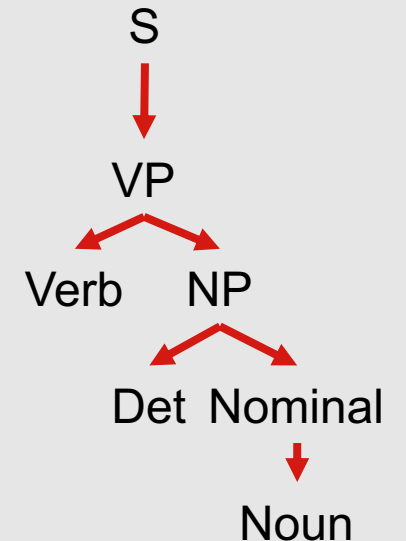
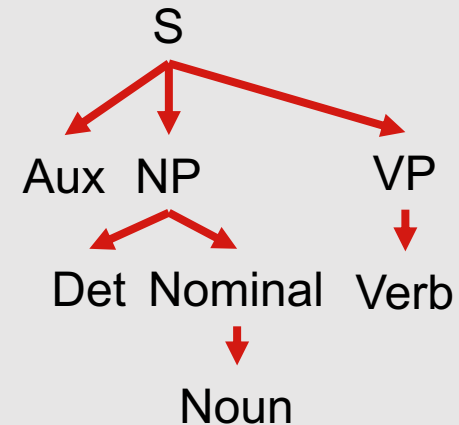
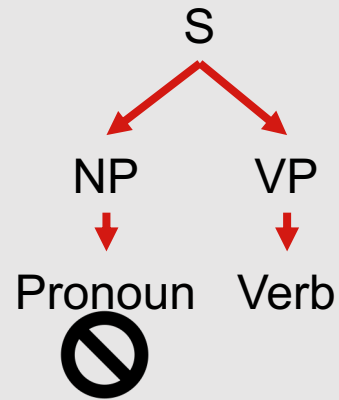


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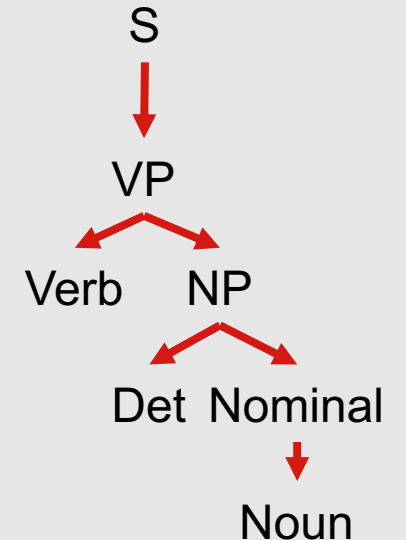
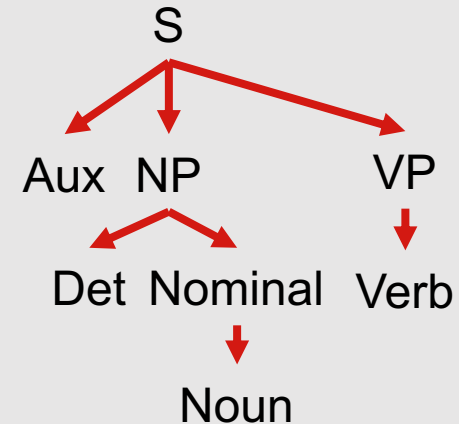
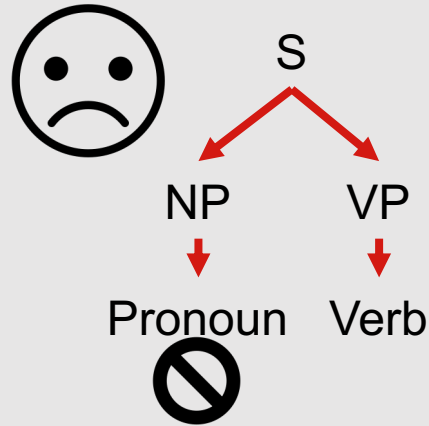
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Noun → book | flight | meal | money  
Verb → **book** | include | prefer  
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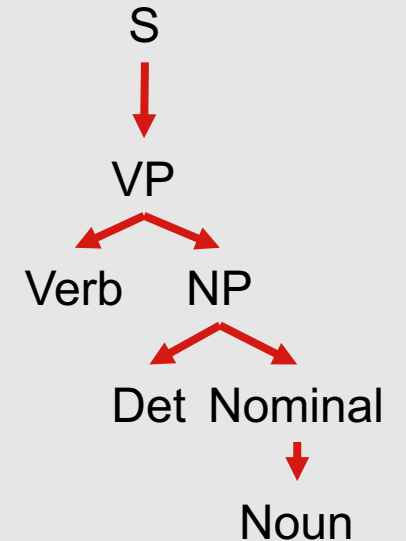
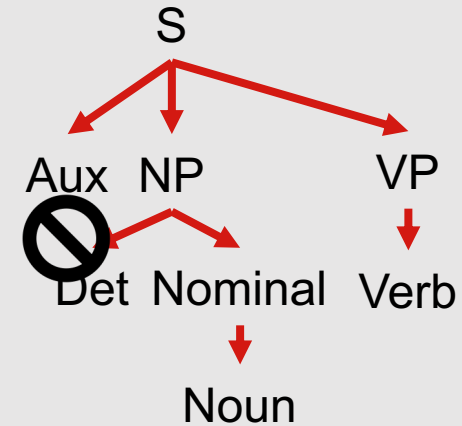
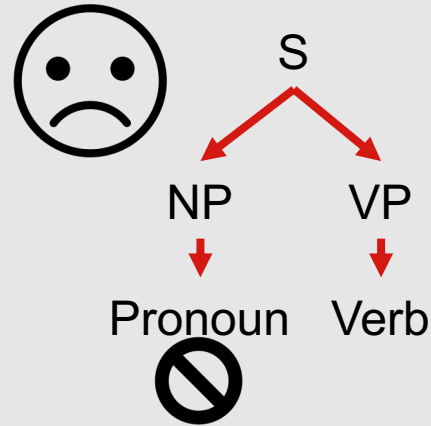
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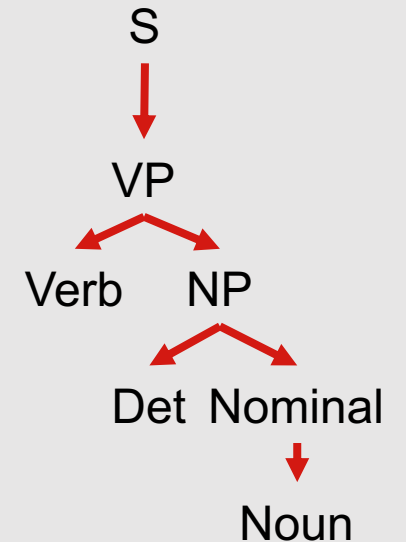
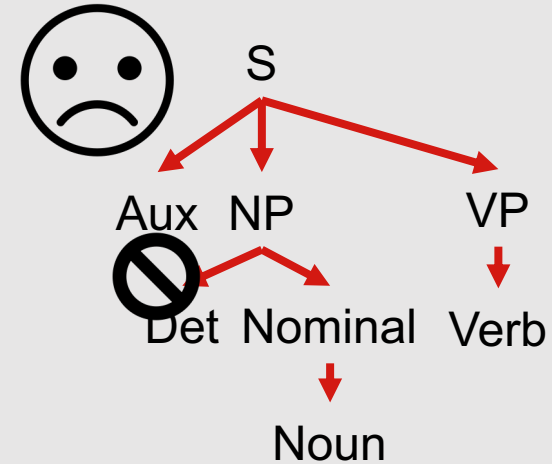
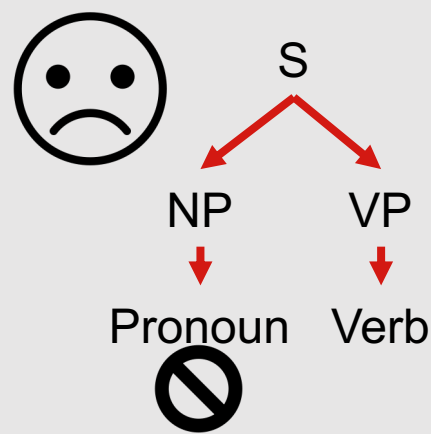
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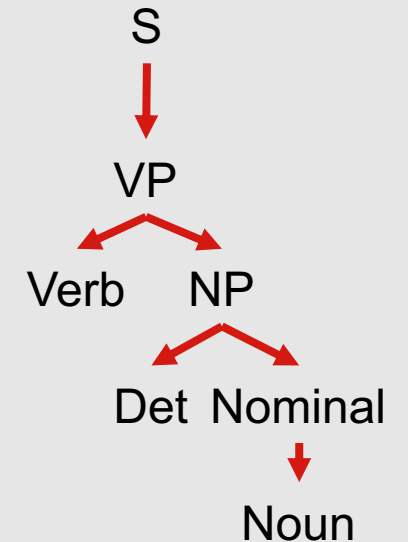
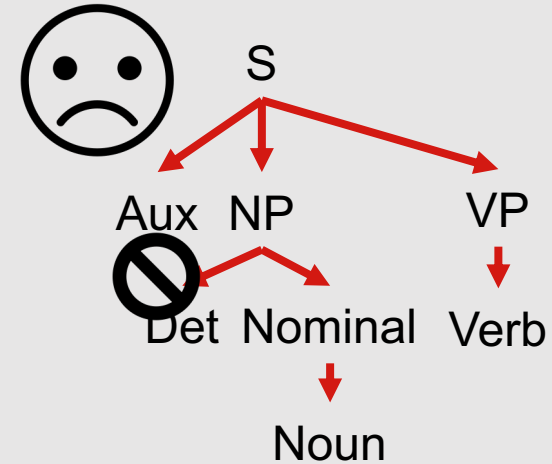
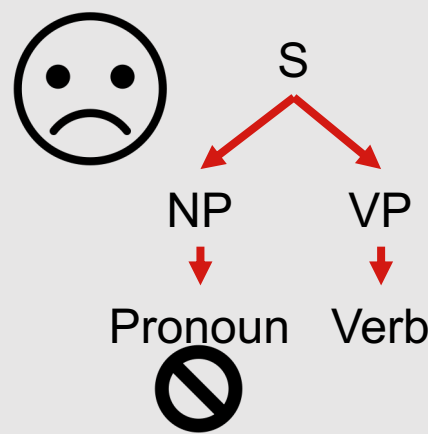
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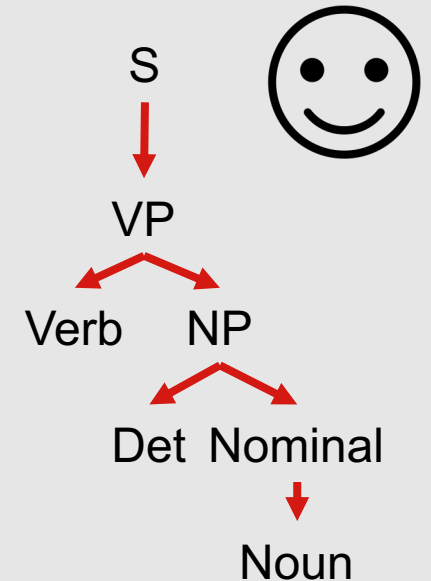
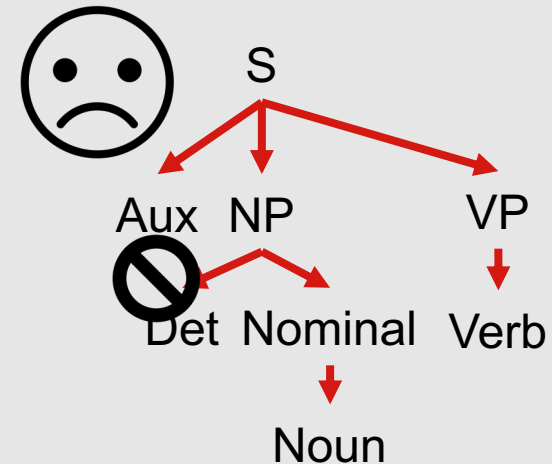
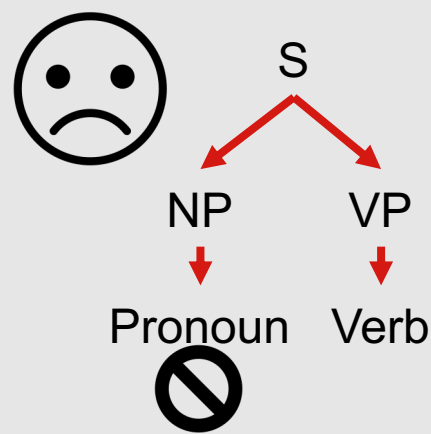
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# Bottom-Up Parsing

- Earliest known parsing algorithm!
- Starts with the words in the input sentence, and tries to build trees from those words up by applying rules from the grammar one at a time
  - Looks for places in the in-progress parse where the righthand side of a production rule might fit
- Success = parser builds a tree rooted in the start symbol **S** that covers all of the input words

# Bottom-Up Parsing: Example

## Input Sentence:

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## Grammar:

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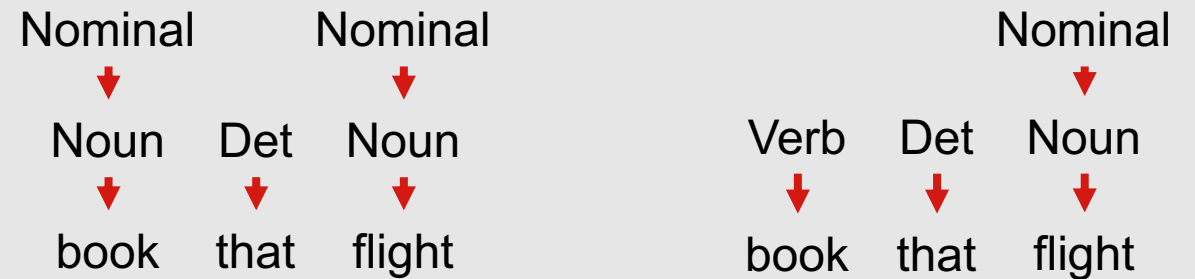
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Noun	Det	Noun	Verb	Det	Noun
↓	↓	↓	↓	↓	↓
book	that	flight	book	that	flight

# Bottom-Up Parsing: Example

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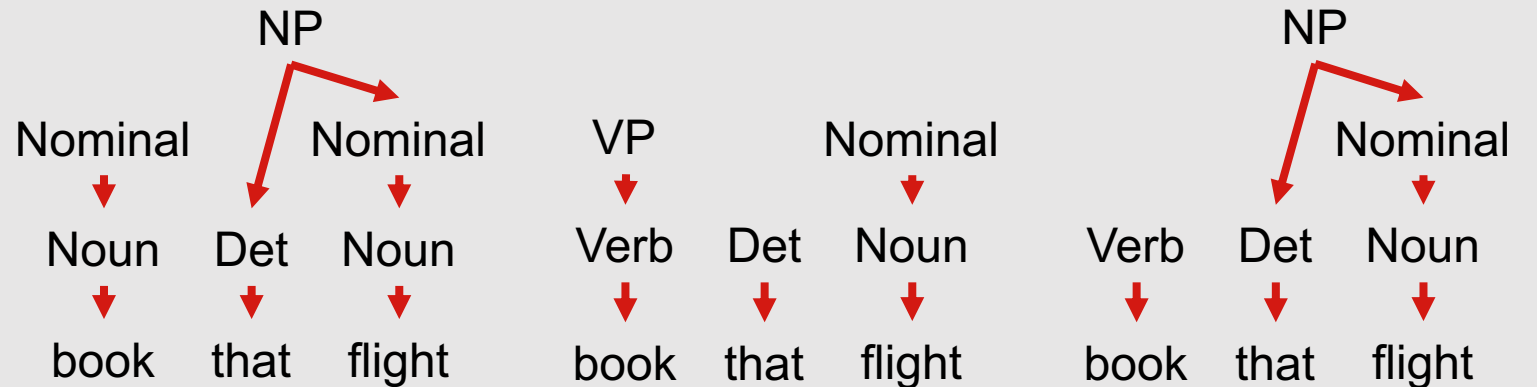




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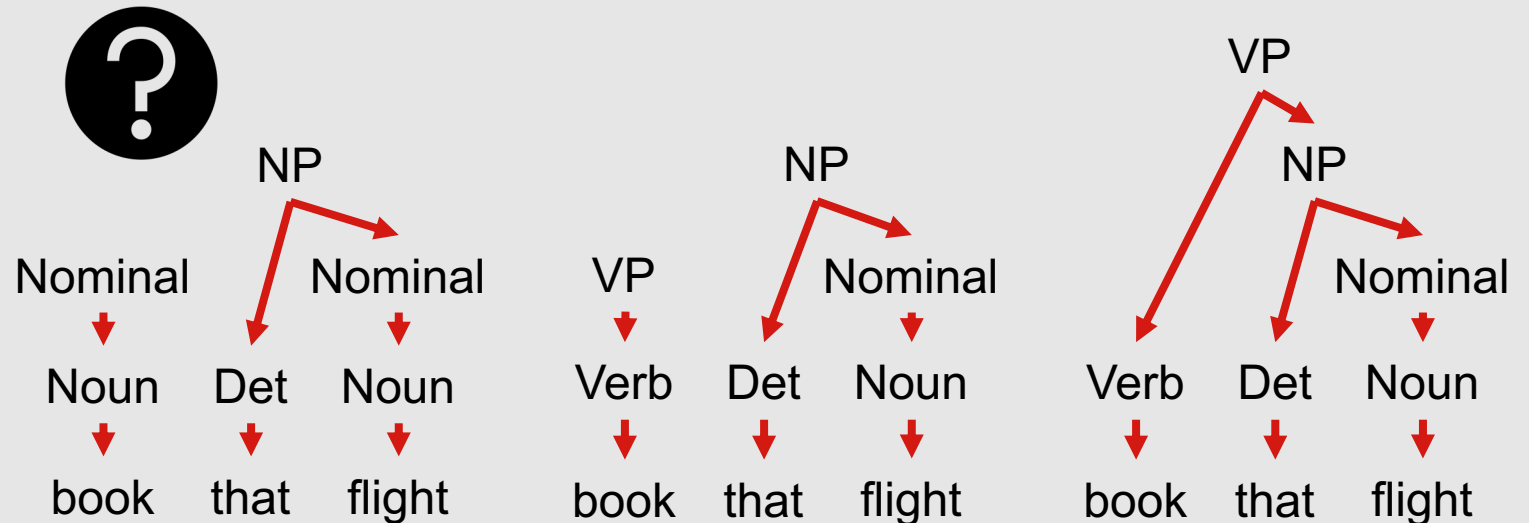
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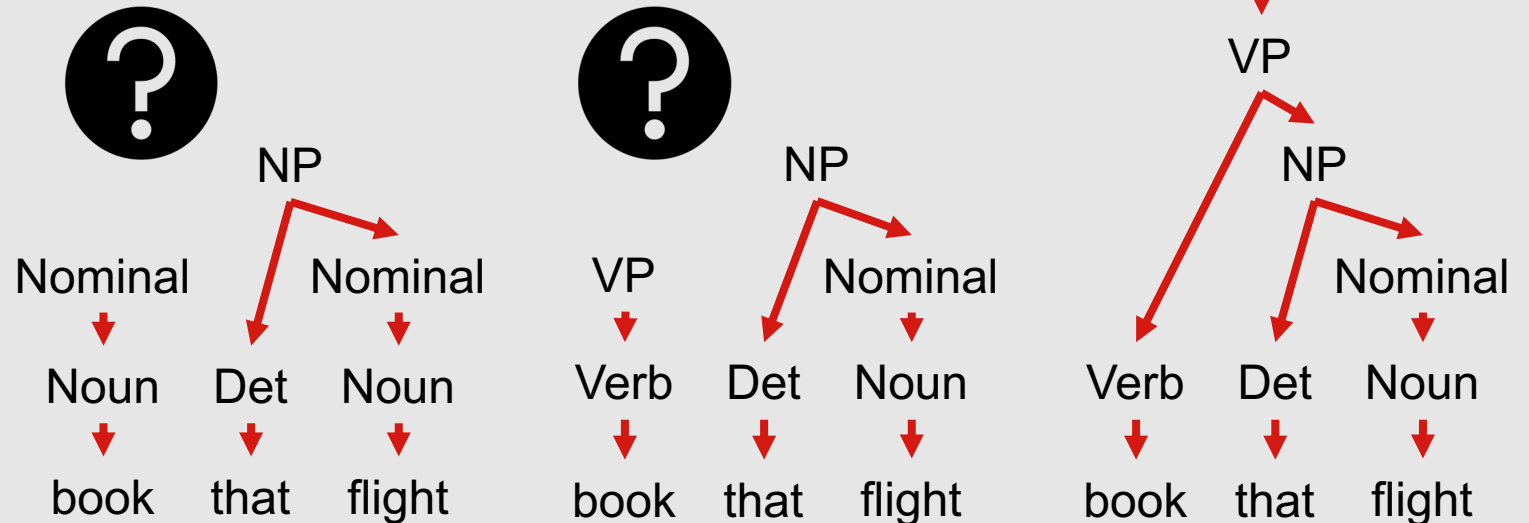
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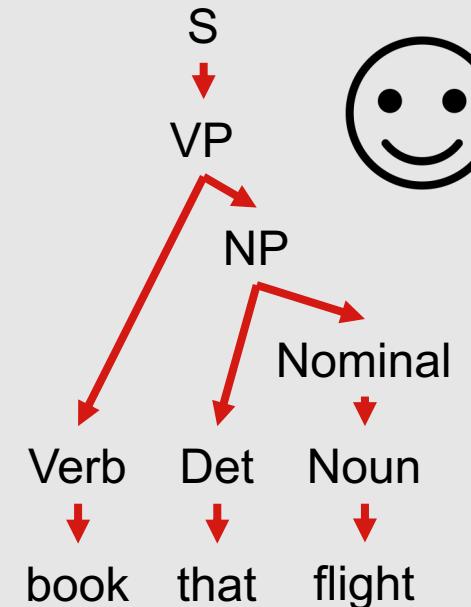
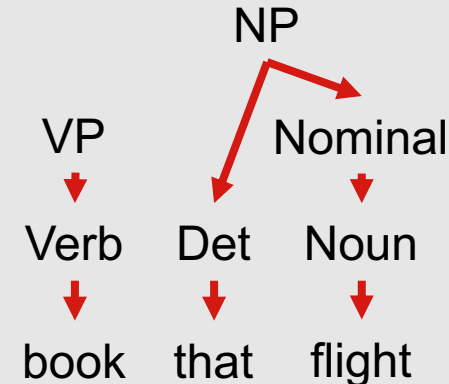
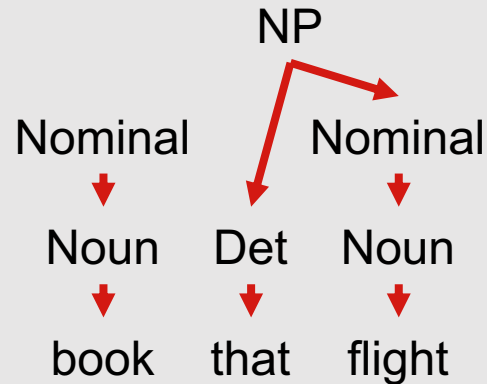
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# Top-Down vs. Bottom-Up Parsing

## Top-Down Parsing

- Pros:
  - Never wastes time exploring trees that cannot result in a sentence
  - Never explores subtrees that cannot fit into a larger valid (i.e., results in a sentence) tree
- Cons:
  - Spends considerable effort on trees that are not consistent with the input

## Bottom-Up Parsing

- Pros:
  - Never suggests trees that are inconsistent with the input
- Cons:
  - Generates many trees and subtrees that cannot result in a valid sentence (according to production rules specified by the grammar)

# More about ambiguity....

- **Structural Ambiguity:** Occurs when a grammar allows for more than one possible parse for a given sentence
- Two Forms:
  - **Attachment Ambiguity:** Occurs when a constituent can be attached to a parse tree at more than one place
    - I eat spaghetti **with chopsticks**.
  - **Coordination Ambiguity:** Occurs when different sets of phrases can be conjoined by a conjunction
    - I grabbed a muffin from the table marked “nut-free scones **and** muffins,” hoping I’d parsed the sign correctly.

# Remember ...local ambiguity can also exist.

Noun    Det    Noun  
↓        ↓        ↓  
book    that    flight

Verb    Det    Noun  
↓        ↓        ↓  
book    that    flight

- Det → that | this | a
- Noun → **book** | flight | meal | money
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# All of this ambiguity can lead to really complex search spaces!

- **Backtracking** approaches expand the search space incrementally, systematically exploring one state at a time
- When they arrive at trees inconsistent with the input, they return to an unexplored alternative
- However, in doing so they tend to discard valid subtrees ...this means that time-consuming work needs to be repeated
- More efficient approach?
  - **Dynamic programming**



# Dynamic Programming Parsing Methods

- **Tables store subtrees for constituents as they are discovered**
- Solves:
  - Re-parsing problem
  - (Partially) ambiguity problem, since the table implicitly stores all possible parses

# Dynamic Programming Parsing Methods

- Most widely used methods:
  - Cocke-Kasami-Younger (**CKY**) algorithm
  - **Earley** algorithm
  - **Chart parsing**

# CKY Algorithm

- One of the earliest recognition and parsing algorithms
- **Bottom-up dynamic programming**
- Standard version can only recognize CFGs in **Chomsky Normal Form (CNF)**

# Chomsky Normal Form

- Grammars are restricted to production rules of the form:
  - $A \rightarrow BC$
  - $A \rightarrow w$
- This means that the righthand side of each rule must expand to either two non-terminals or a single terminal
- Any CFG can be converted to a corresponding CNF grammar that accepts exactly the same set of strings as the original grammar!

# How does this conversion work?

- Three situations we need to address:
  1. Production rules that mix terminals and non-terminals on the righthand side
  2. Production rules that have a single non-terminal on the righthand side (**unit productions**)
  3. Production rules that have more than two non-terminals on the righthand side
- Situation #1: **Introduce a dummy non-terminal that covers only the original terminal**
  - $\text{INF-VP} \rightarrow \text{to VP}$  could be replaced with  $\text{INF-VP} \rightarrow \text{TO VP}$  and  $\text{TO} \rightarrow \text{to}$
- Situation #2: **Replace the non-terminals with the non-unit production rules to which they eventually lead**
  - $A \rightarrow B$  and  $B \rightarrow w$  could be replaced with  $A \rightarrow w$
- Situation #3: **Introduce new non-terminals that spread longer sequences over multiple rules**
  - $A \rightarrow B C D$  could be replaced with  $A \rightarrow B X1$  and  $X1 \rightarrow C D$

# CNF Conversion: Example

- $S \rightarrow NP VP$
- $S \rightarrow Aux NP VP$
- $S \rightarrow VP$
- $NP \rightarrow Pronoun$
- $NP \rightarrow Proper-Noun$
- $NP \rightarrow Det Nominal$
- $Nominal \rightarrow Noun$
- $Nominal \rightarrow Nominal Noun$
- $Nominal \rightarrow Nominal PP$
- $VP \rightarrow Verb$
- $VP \rightarrow Verb NP$
- $VP \rightarrow Verb NP PP$
- $VP \rightarrow Verb PP$
- $VP \rightarrow VP PP$
- $PP \rightarrow Preposition NP$

Original	CNF
$S \rightarrow NP VP$	$S \rightarrow NP VP$
$S \rightarrow Aux NP VP$	$S \rightarrow X1 VP$
	$X1 \rightarrow Aux NP$
$S \rightarrow VP$	$S \rightarrow book \mid include \mid prefer$
	$S \rightarrow Verb NP$
	$S \rightarrow X2 PP$
	$X2 \rightarrow Verb NP$
	$S \rightarrow Verb PP$
	$S \rightarrow VP PP$

# CKY Algorithm

- With the grammar in CNF, each non-terminal node above the POS level of the parse tree will have exactly two children
- Thus, a two-dimensional matrix can be used to encode the tree structure
- For sentence of length  $n$ , work with upper-triangular portion of  $(n+1) \times (n+1)$  matrix
- Each cell  $[i,j]$  contains a set of non-terminals that represent all constituents spanning positions  $i$  through  $j$  of the input
  - Cell that represents the entire input resides in position  $[0,n]$

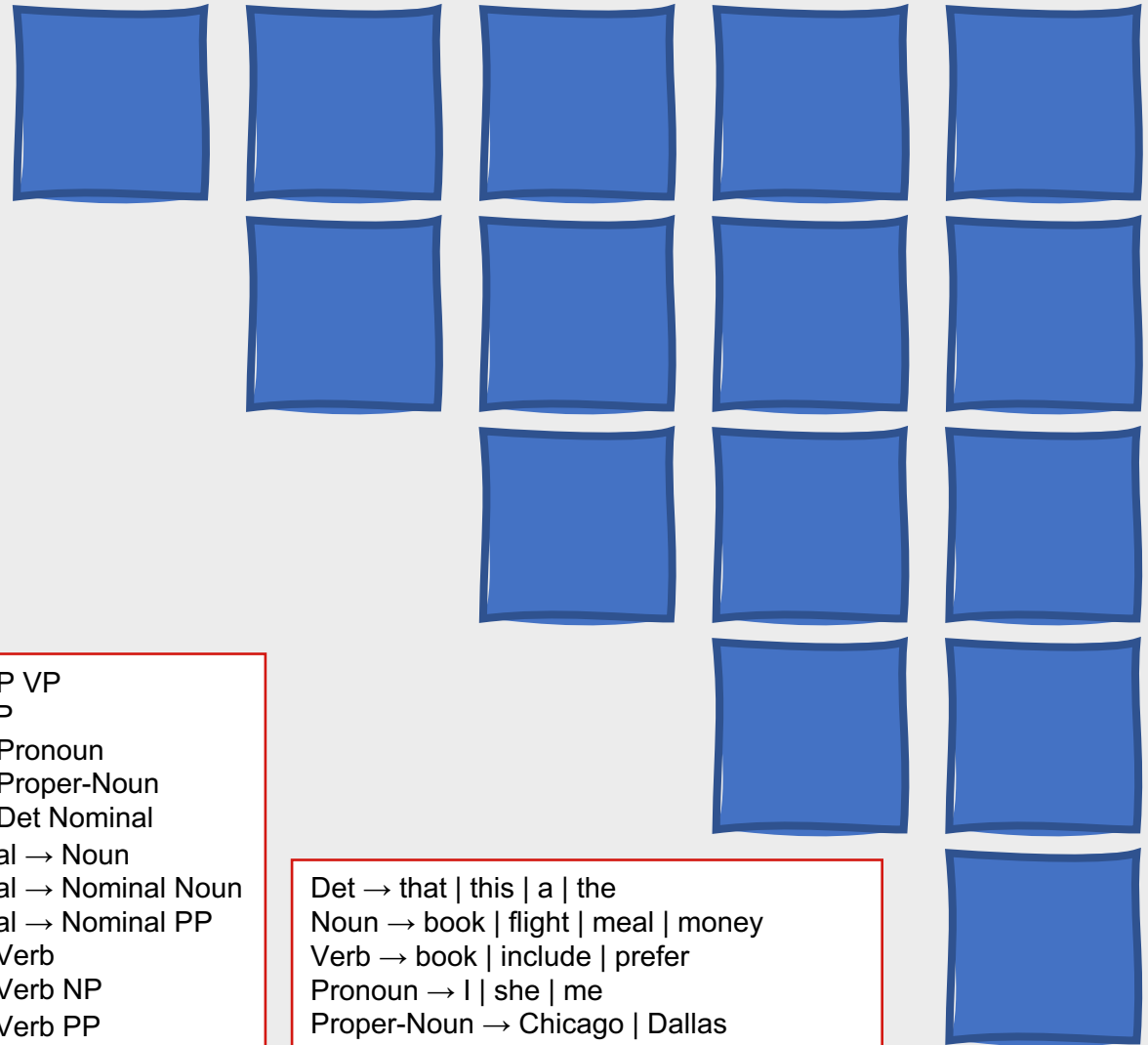
# CKY Algorithm

- Non-terminal entries: For each constituent  $[i,j]$ , there is a position,  $k$ , where the constituent can be split into two parts such that  $i < k < j$ 
  - $[i,k]$  must lie to the left of  $[i,j]$  somewhere along row  $i$ , and  $[k,j]$  must lie beneath it along column  $j$
- To fill in the parse table, we proceed in a bottom-up fashion so when we fill a cell  $[i,j]$ , the cells containing the parts that could contribute to this entry have already been filled



# CKY Algorithm: Example

Book      the      flight      through      Chicago



$S \rightarrow NP VP$   
 $S \rightarrow VP$   
 $NP \rightarrow Pronoun$   
 $NP \rightarrow Proper-Noun$   
 $NP \rightarrow Det Nominal$   
 $Nominal \rightarrow Noun$   
 $Nominal \rightarrow Nominal Noun$   
 $Nominal \rightarrow Nominal PP$   
 $VP \rightarrow Verb$   
 $VP \rightarrow Verb NP$   
 $VP \rightarrow Verb PP$   
 $VP \rightarrow VP PP$   
 $PP \rightarrow Preposition NP$

$Det \rightarrow that \mid this \mid a \mid the$   
 $Noun \rightarrow book \mid flight \mid meal \mid money$   
 $Verb \rightarrow book \mid include \mid prefer$   
 $Pronoun \rightarrow I \mid she \mid me$   
 $Proper-Noun \rightarrow Chicago \mid Dallas$   
 $Aux \rightarrow does$   
 $Preposition \rightarrow from \mid to \mid on \mid near \mid through$

# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

S → NP VP  
 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → **book** | flight | meal | money  
 Verb → **book** | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

S → NP VP  
 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
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# CKY Algorithm: Example

Det → that | this | a | **the**  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

S → NP VP  
 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
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# CKY Algorithm: Example

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 Noun → book | **flight** | meal | money  
 Verb → book | include | prefer  
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 Preposition → from | to | on | near | through

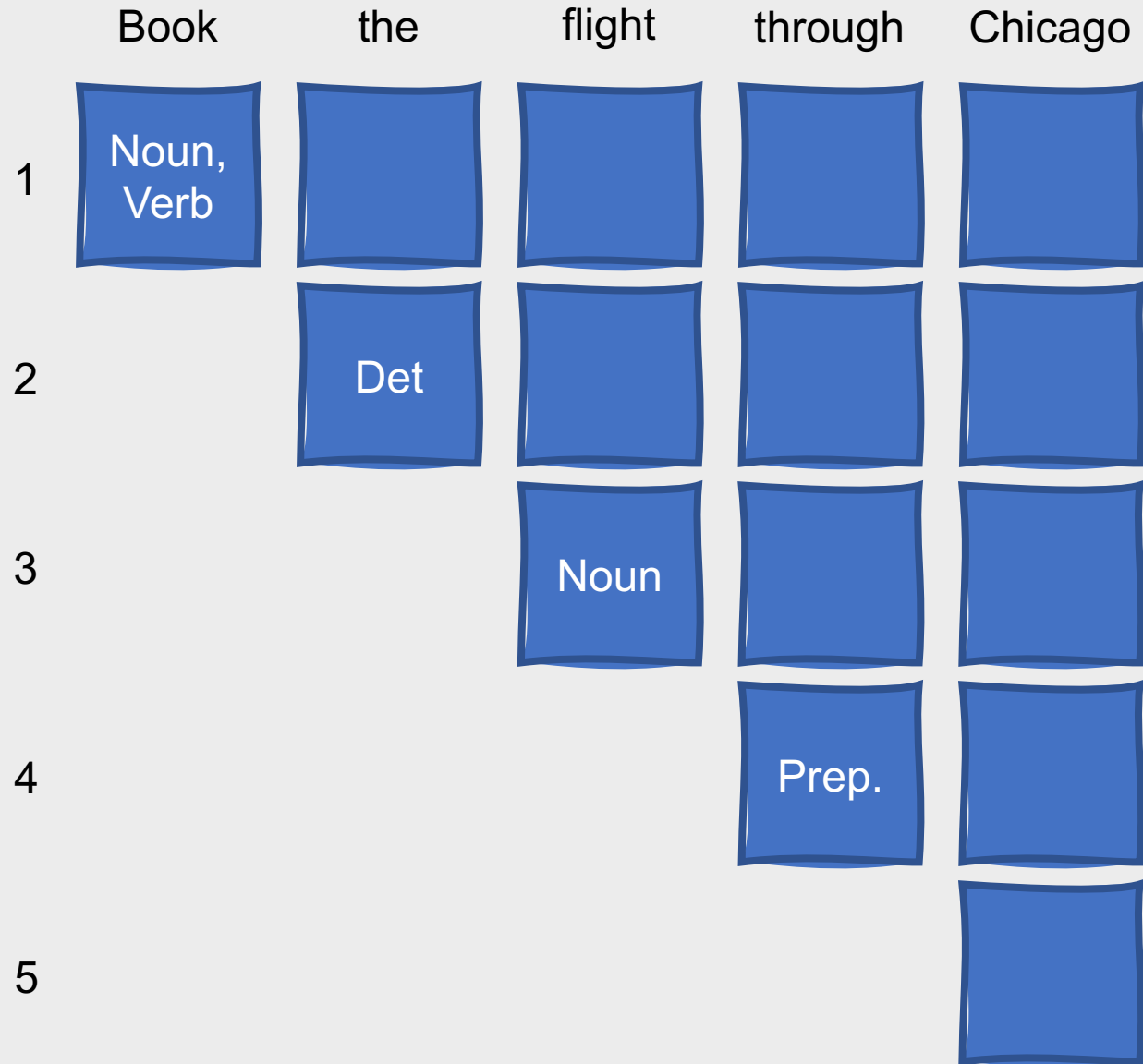
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 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
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# CKY Algorithm: Example

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 Noun → book | flight | meal | money  
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 Aux → does  
 Preposition → from | to | on | near | **through**

S → NP VP  
 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
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 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
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# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
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 Pronoun → I | she | me  
 Proper-Noun → **Chicago** | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

S → NP VP  
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 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
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 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

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 Noun → book | flight | meal | money  
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 Aux → does  
 Preposition → from | to | on | near | through

S → NP VP  
 S → VP → Verb → **book** | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → **book** | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → **book** | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP

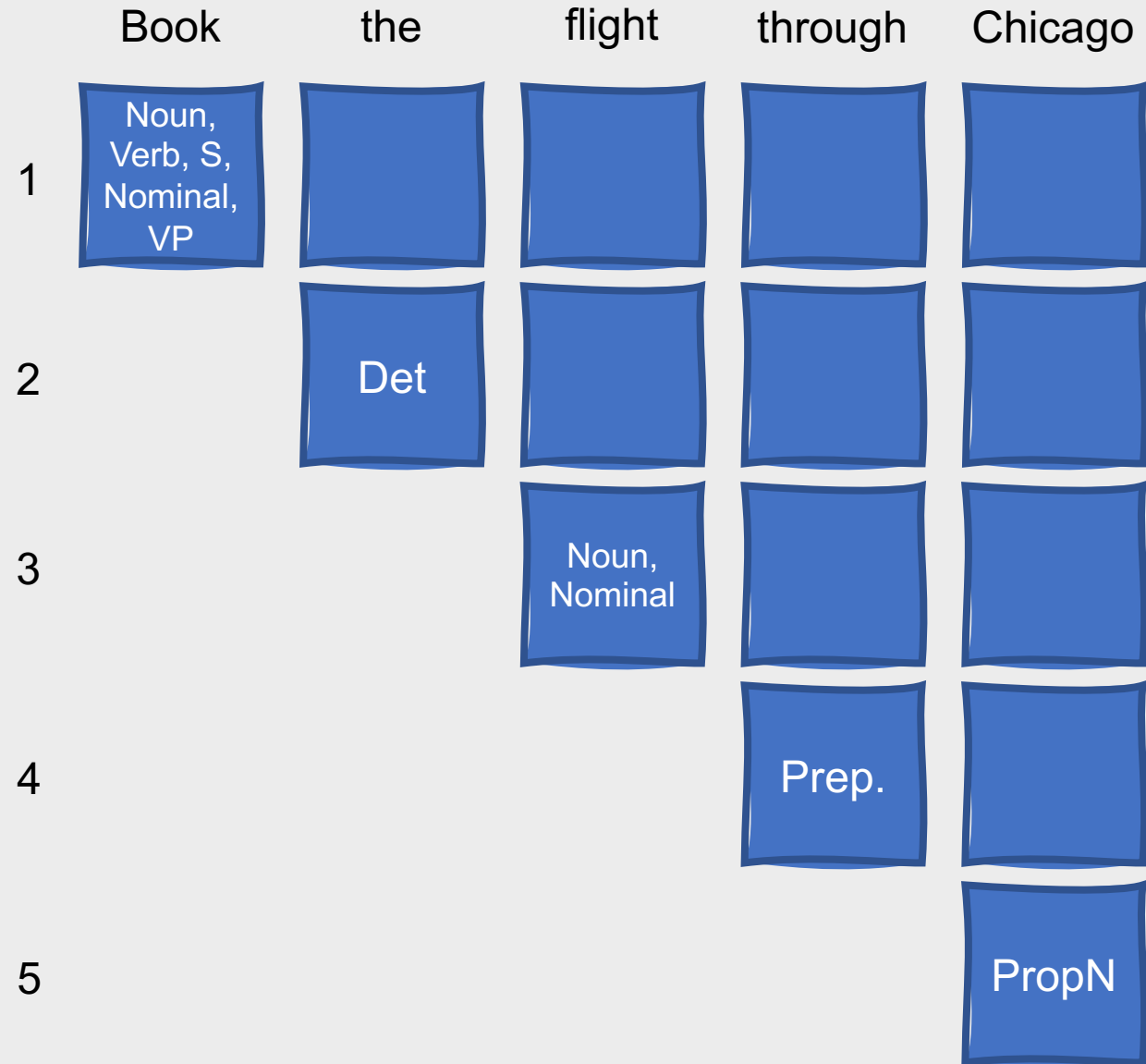




# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

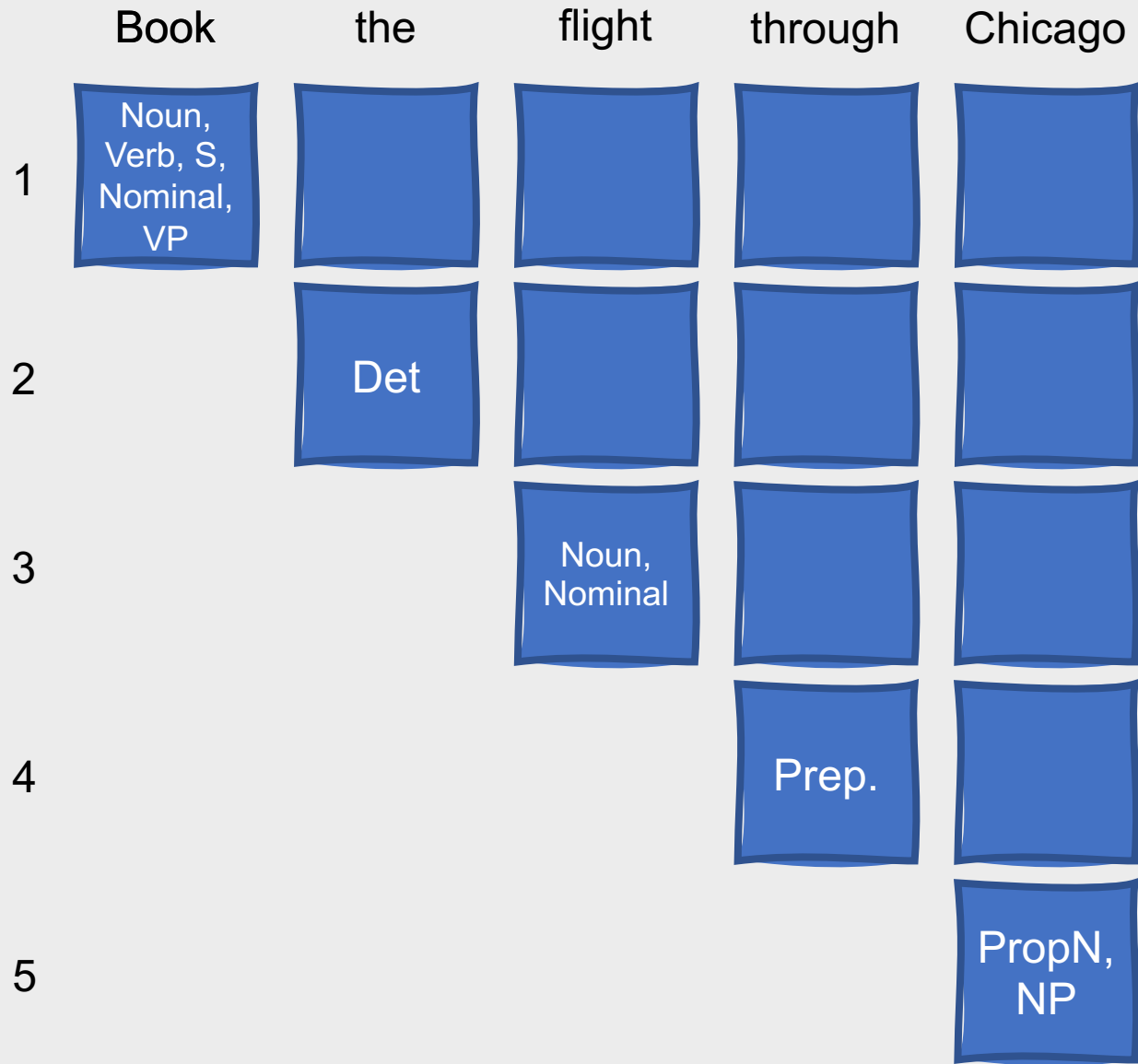
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 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → **book** | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
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 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
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 Aux → does  
 Preposition → from | to | on | near | through

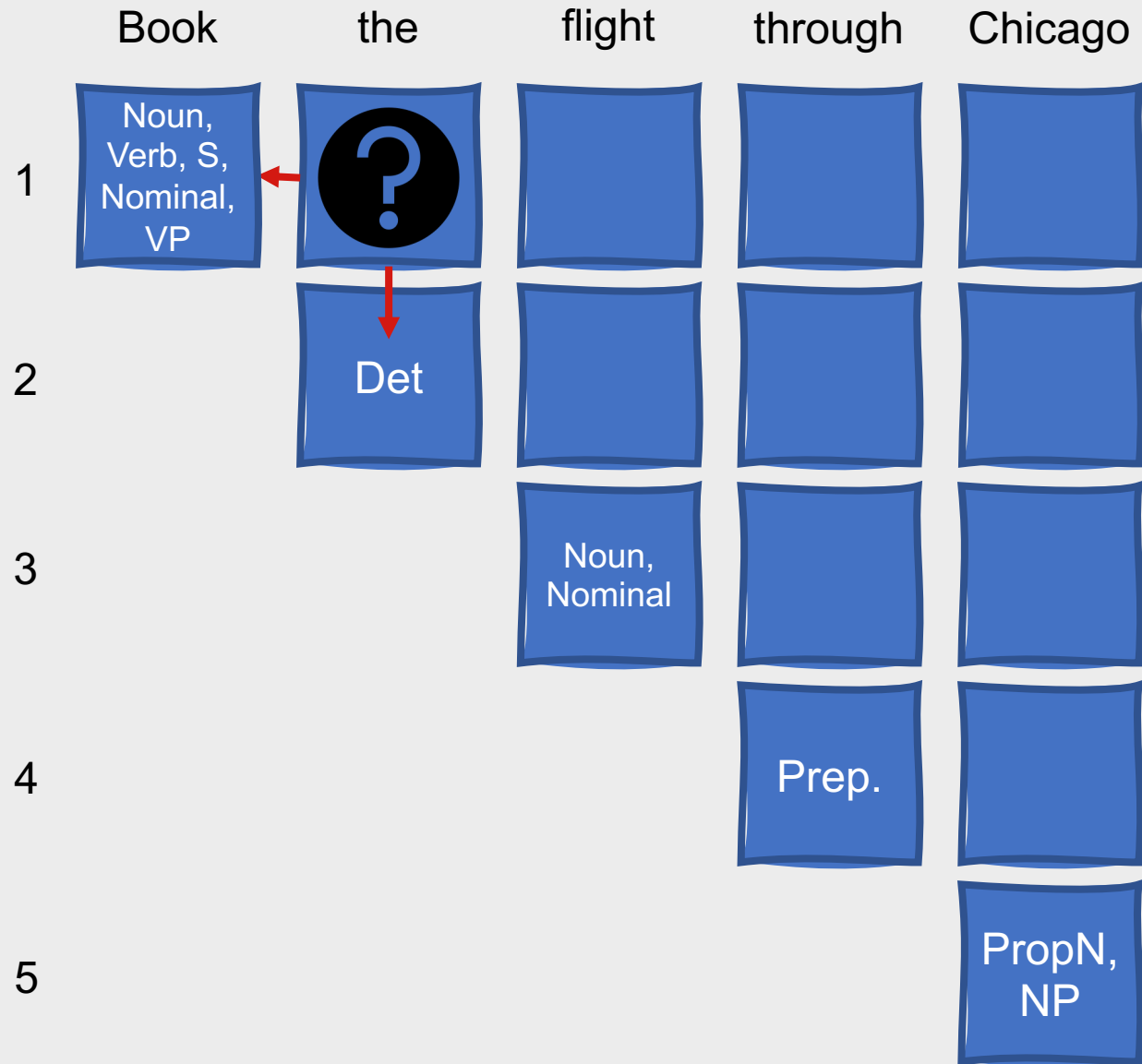
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 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → **Chicago** | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

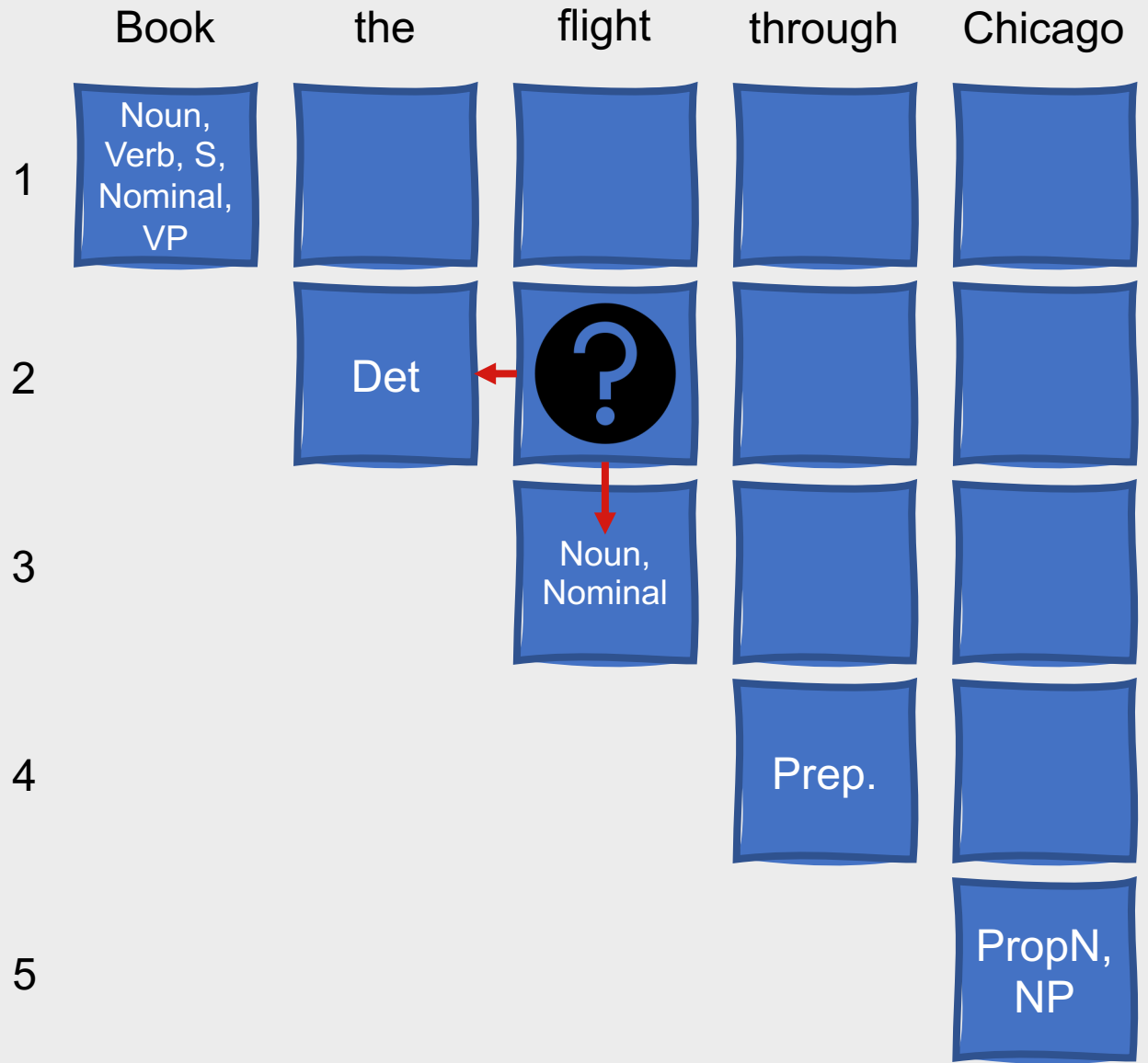
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 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
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 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
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# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
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 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

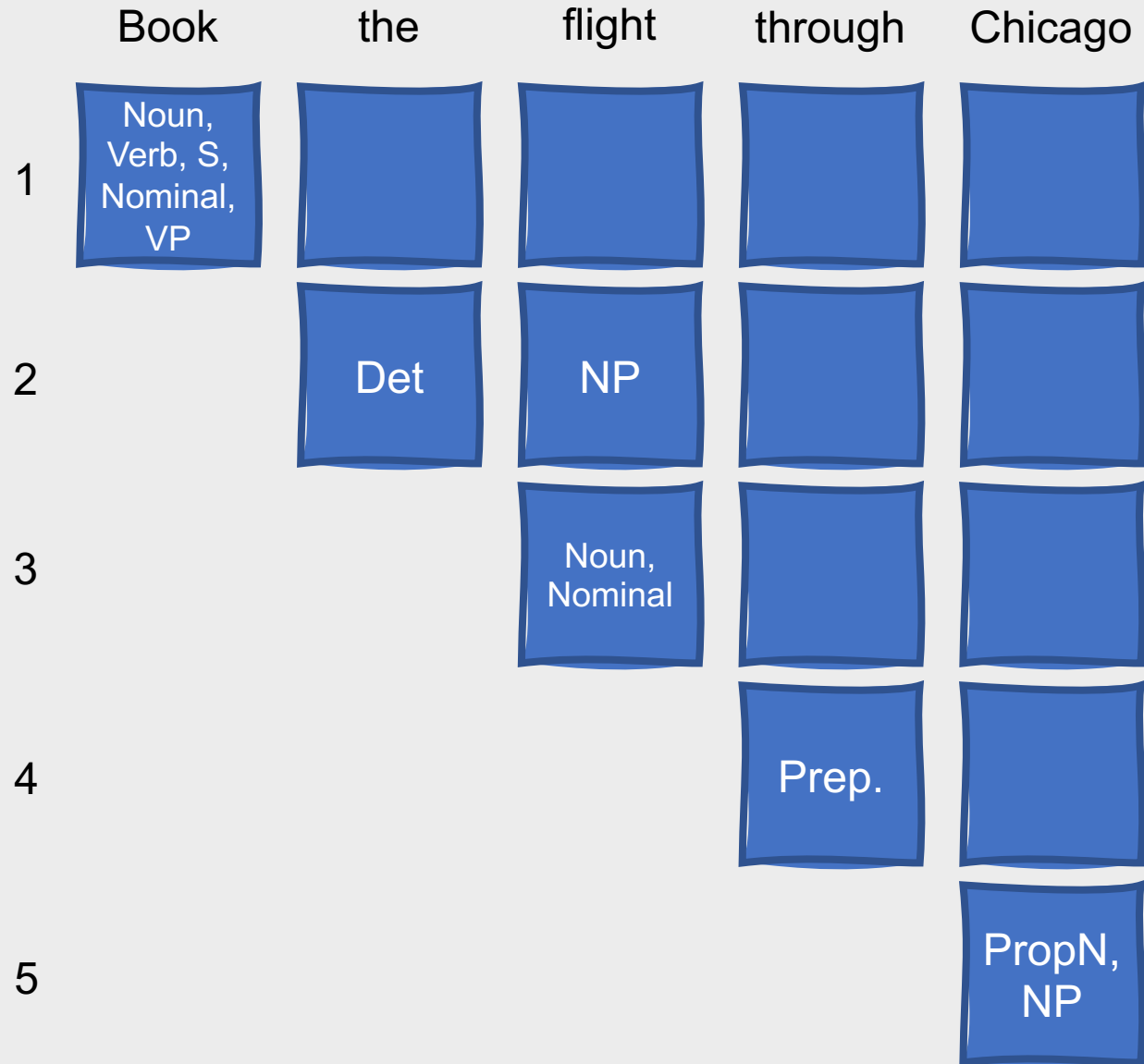
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 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
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 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

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 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
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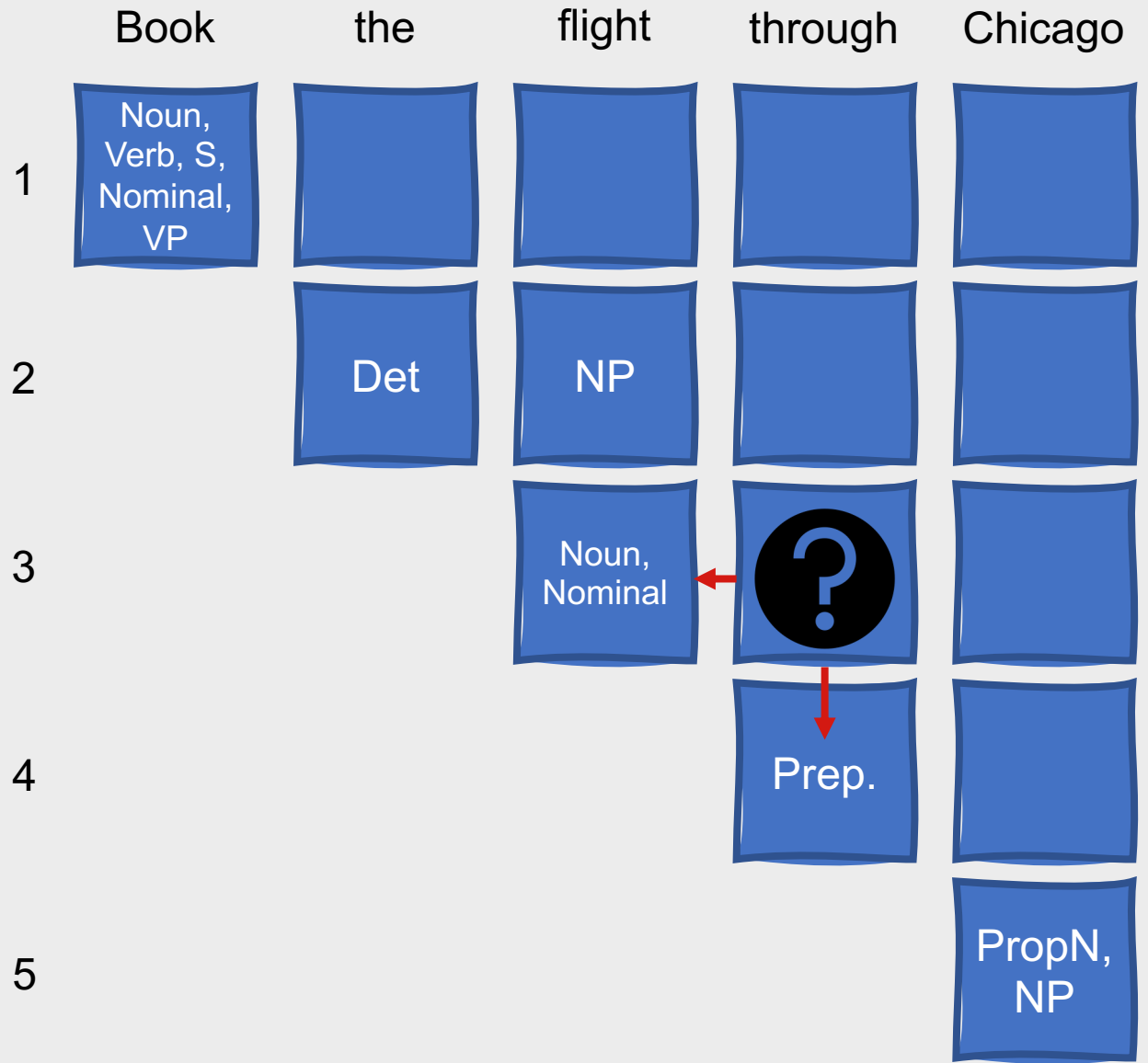
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 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → **Det Nominal**  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
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 Aux → does  
 Preposition → from | to | on | near | through

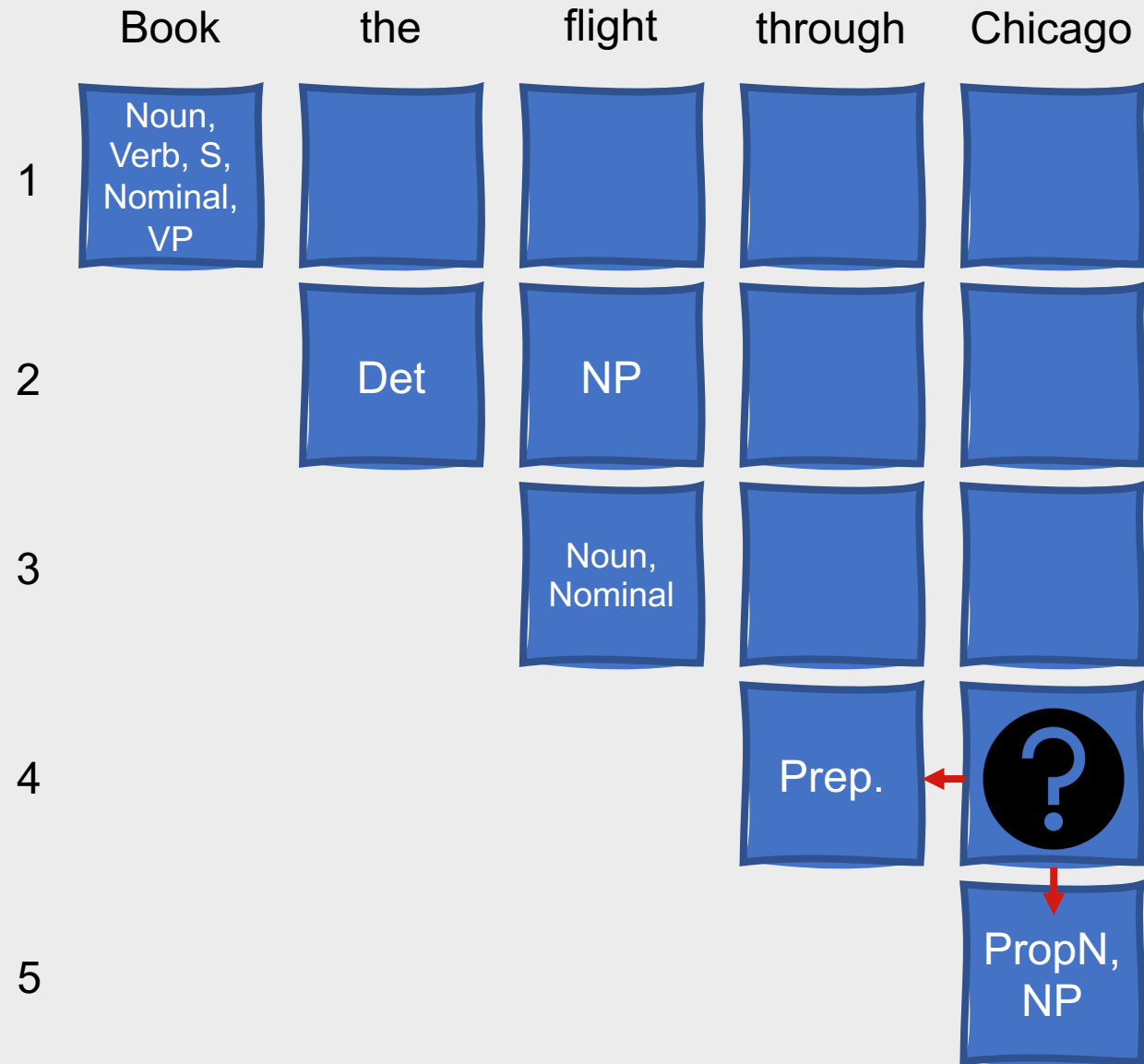
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 Nominal → Noun → book | flight | meal | money  
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 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

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 Noun → book | flight | meal | money  
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 Preposition → from | to | on | near | through

S → NP VP  
 S → VP → Verb → book | include | prefer  
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 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

Det → that | this | a | the  
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 Verb → book | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

S → NP VP  
 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → **Preposition NP**

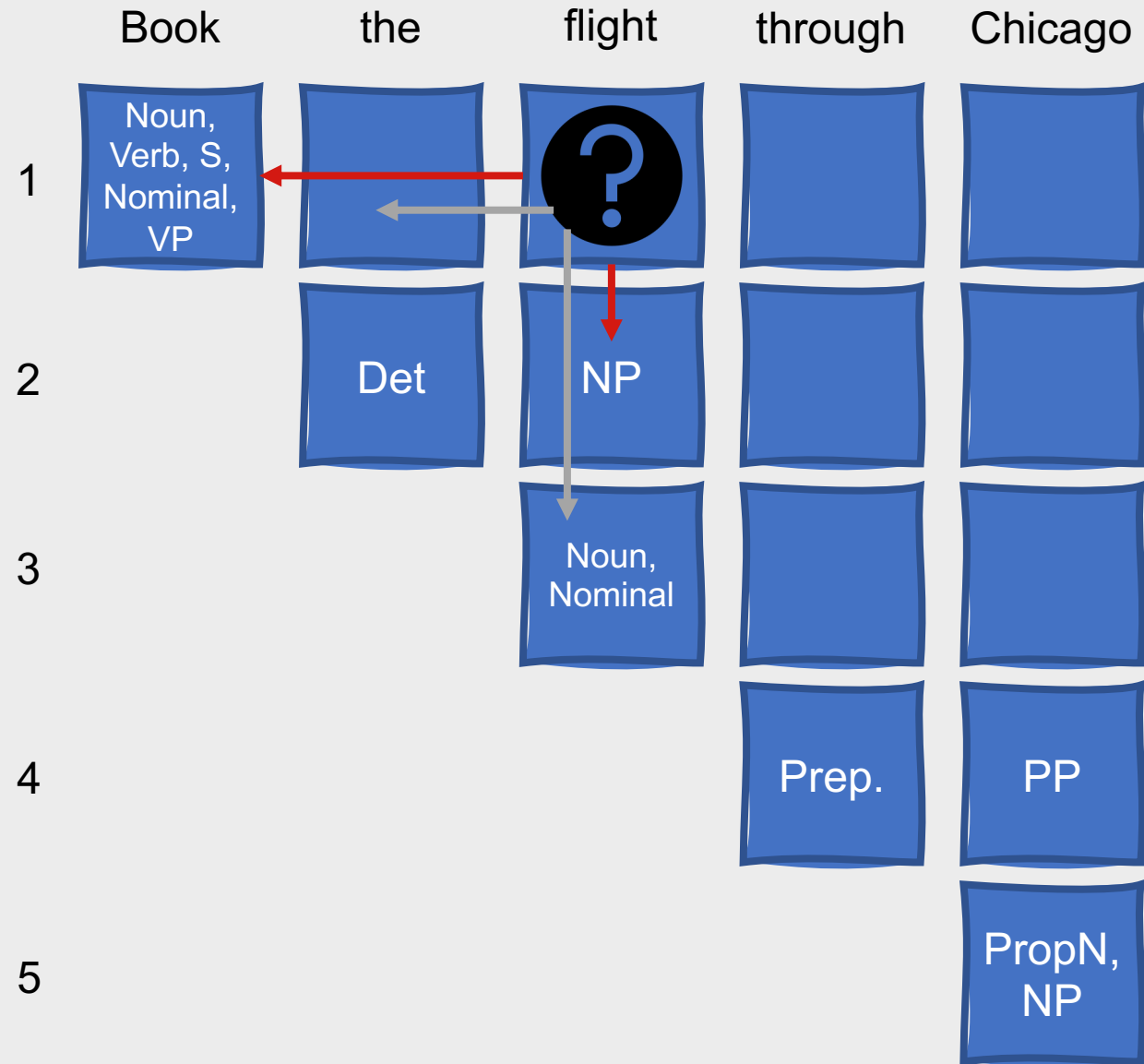




# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
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 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

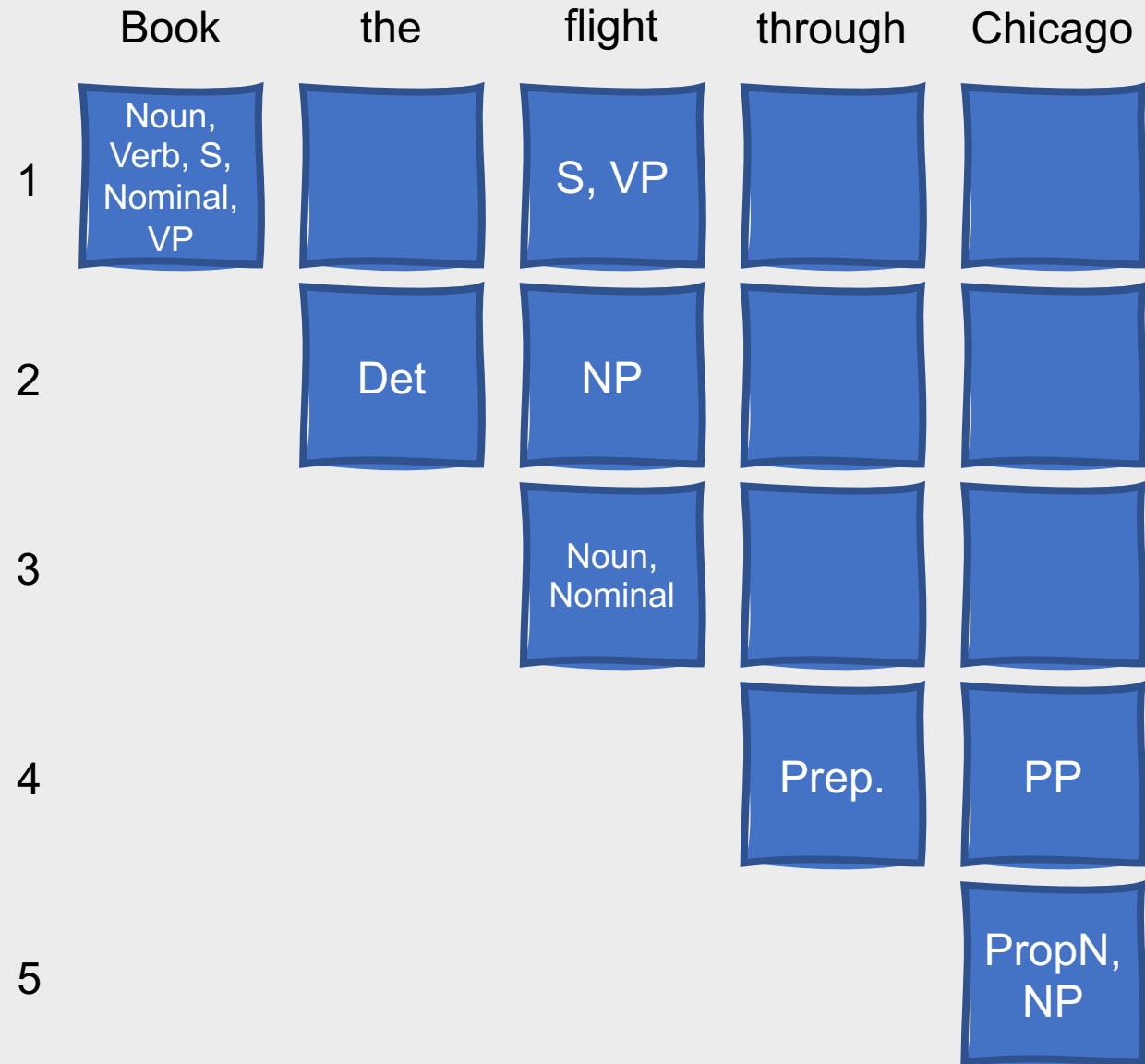
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 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

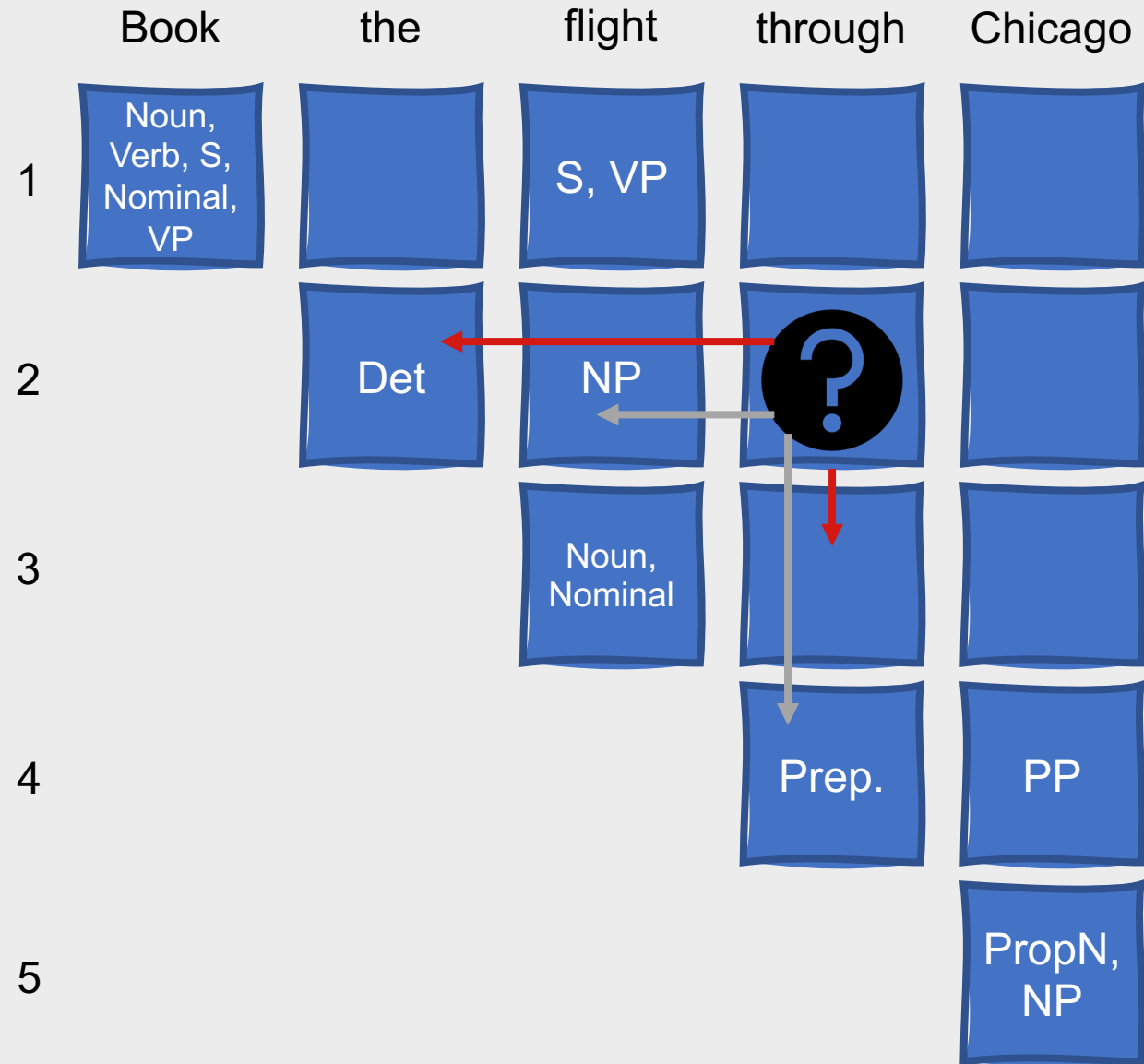
S → NP VP  
 S → **VP** → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → **Verb NP**  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

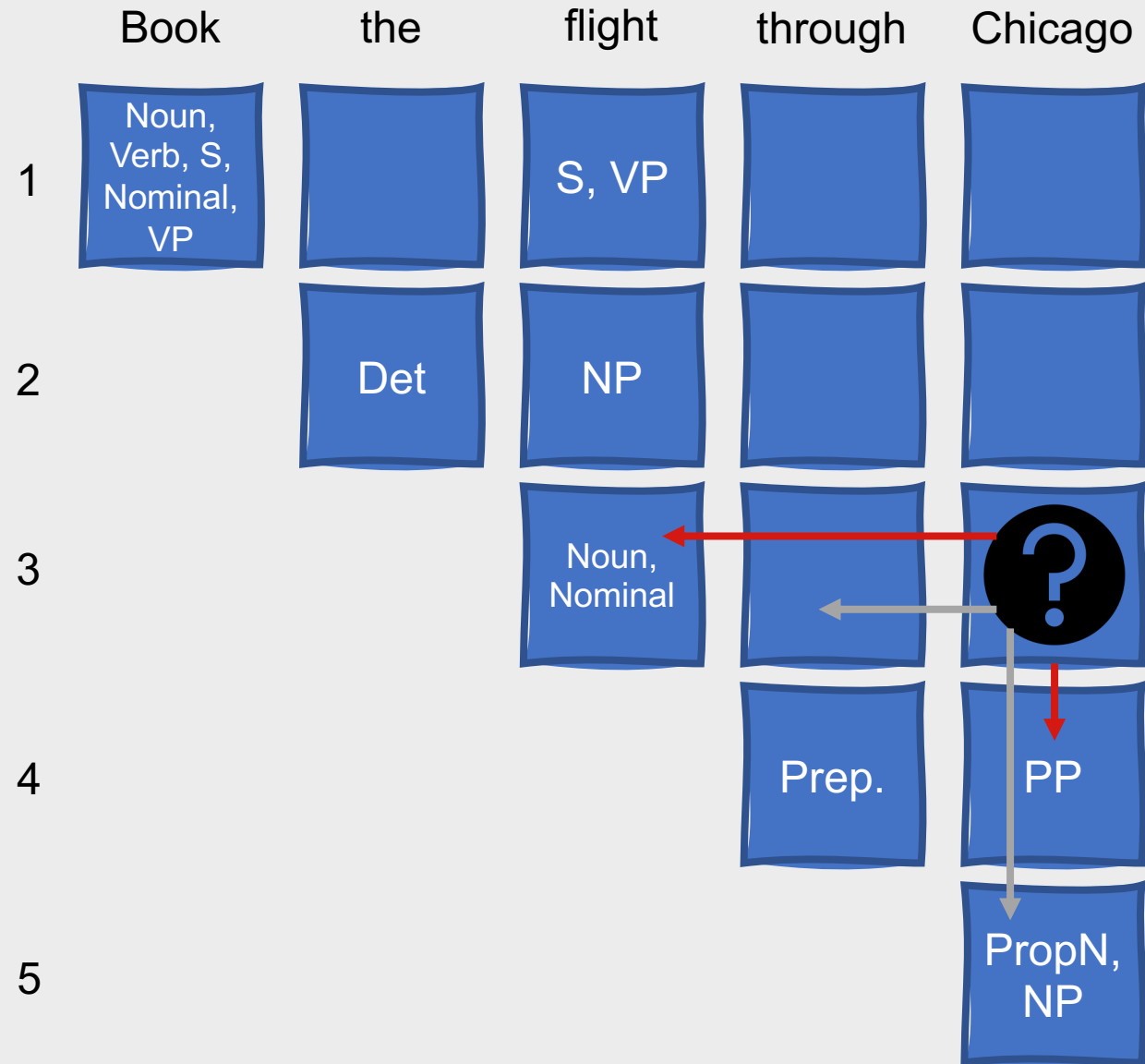
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 NP → Pronoun → I | she | me  
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 NP → Det Nominal  
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 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

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 Noun → book | flight | meal | money  
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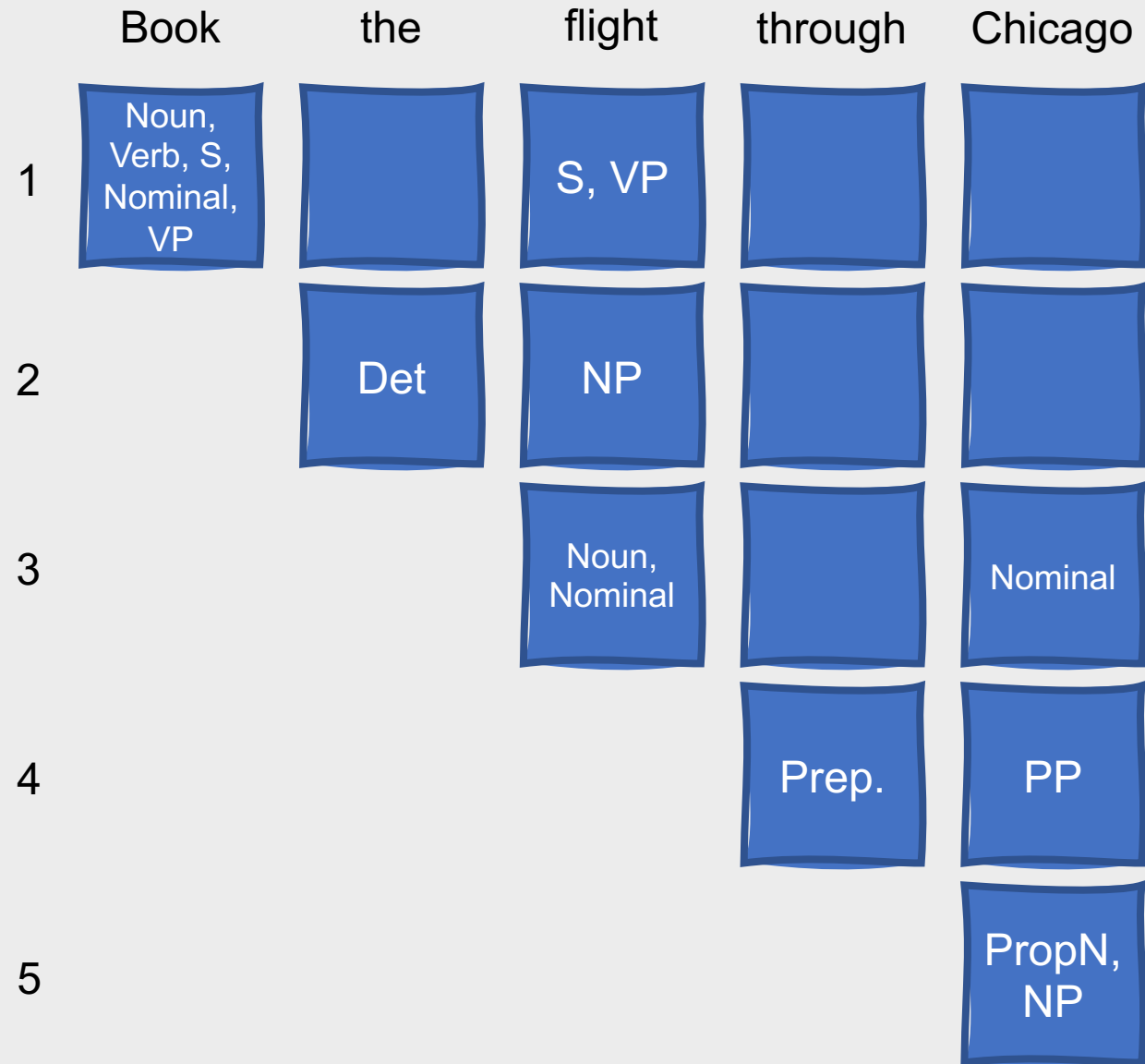
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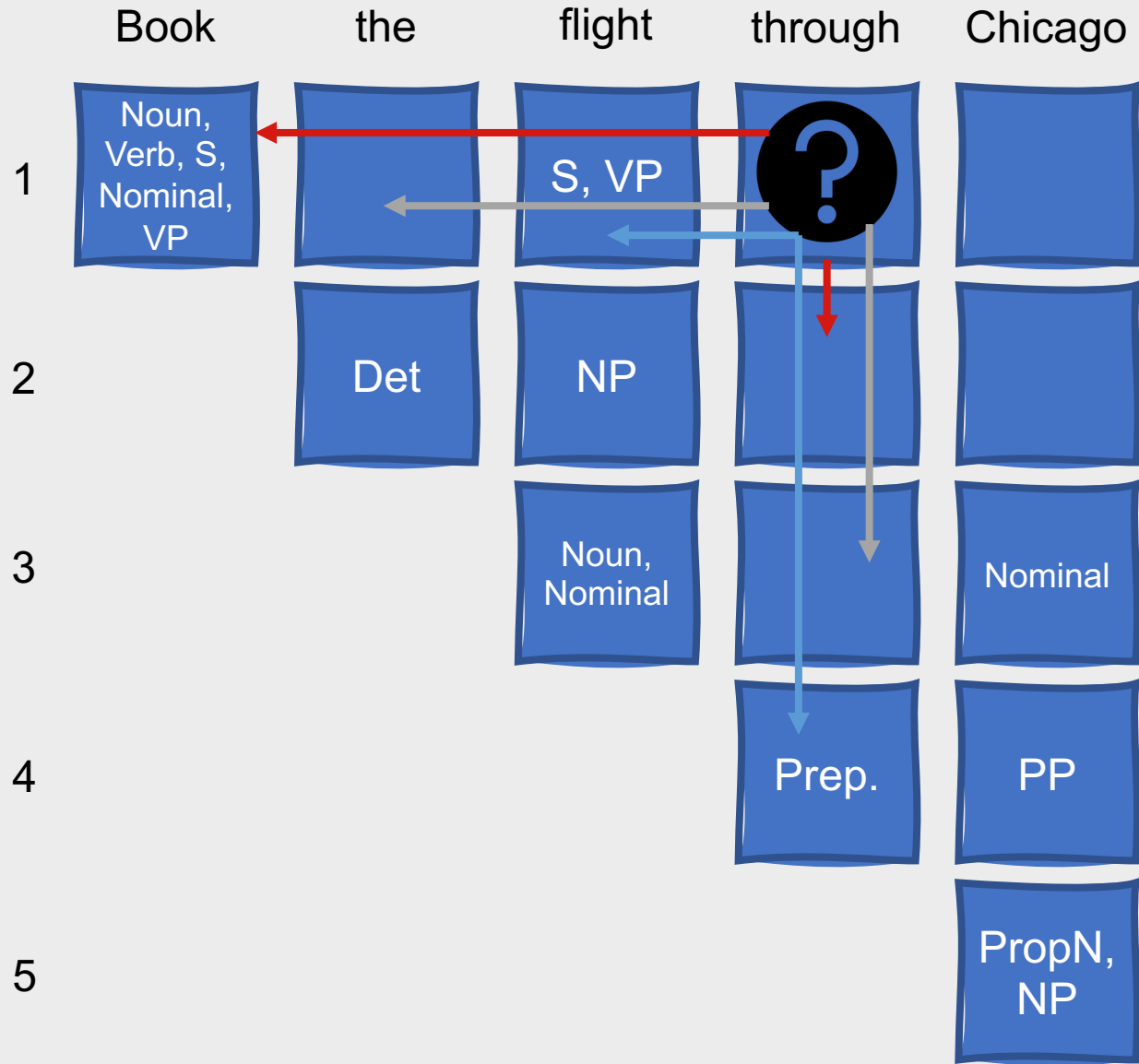
S → NP VP  
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 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → **Nominal PP**  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
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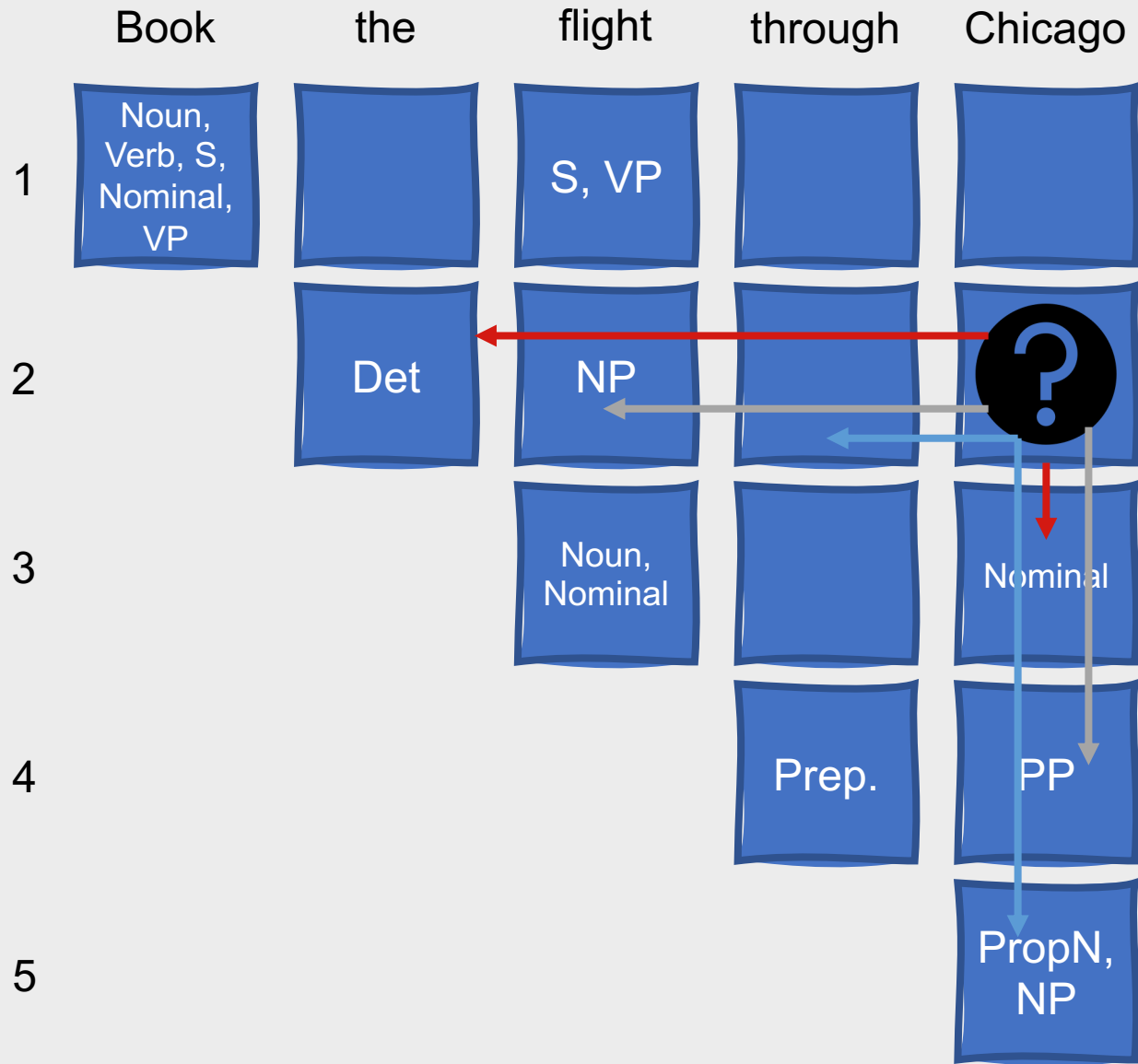
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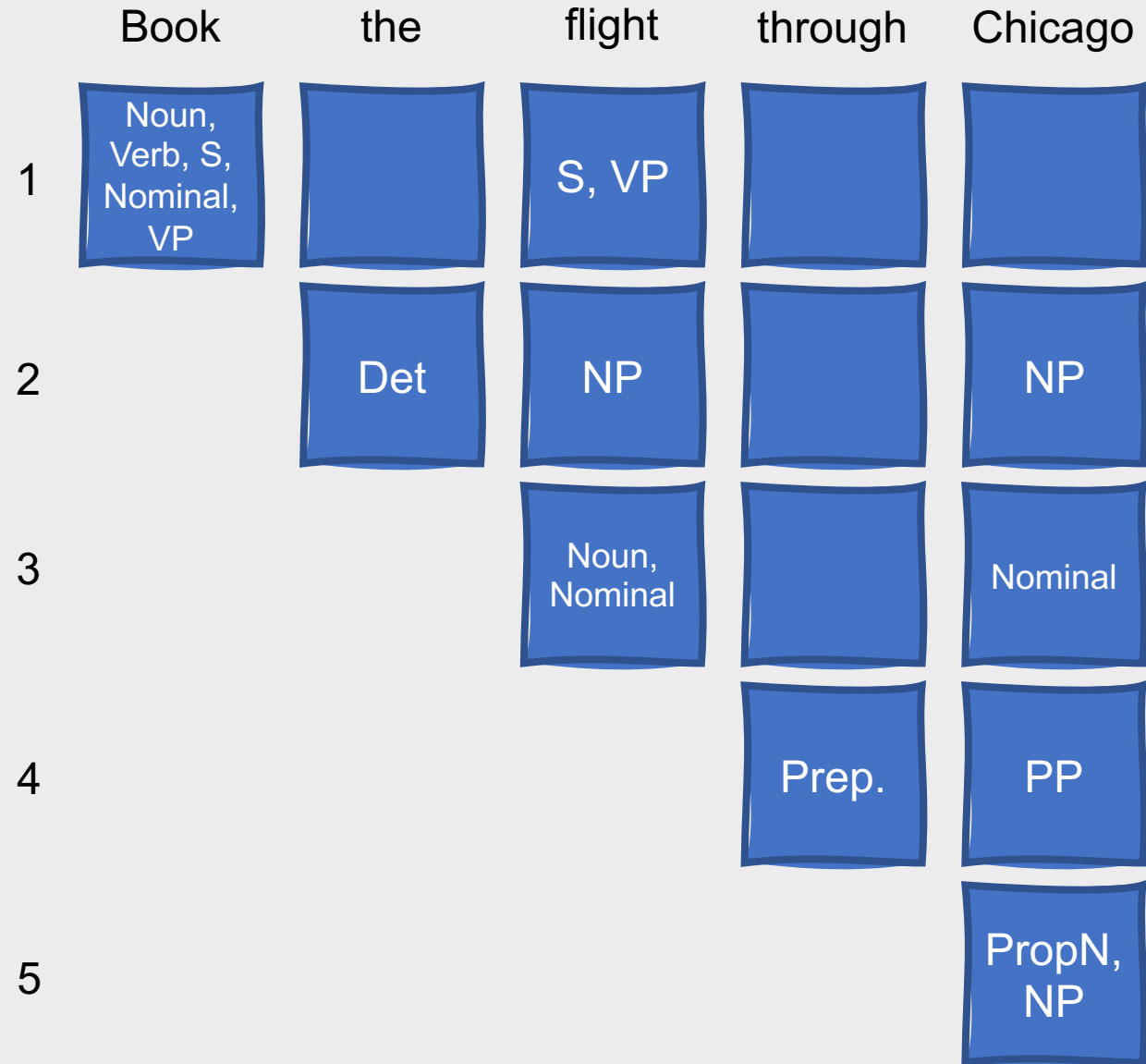
S → NP VP  
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 Preposition → from | to | on | near | through

S → NP VP  
 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → **Det Nominal**  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP

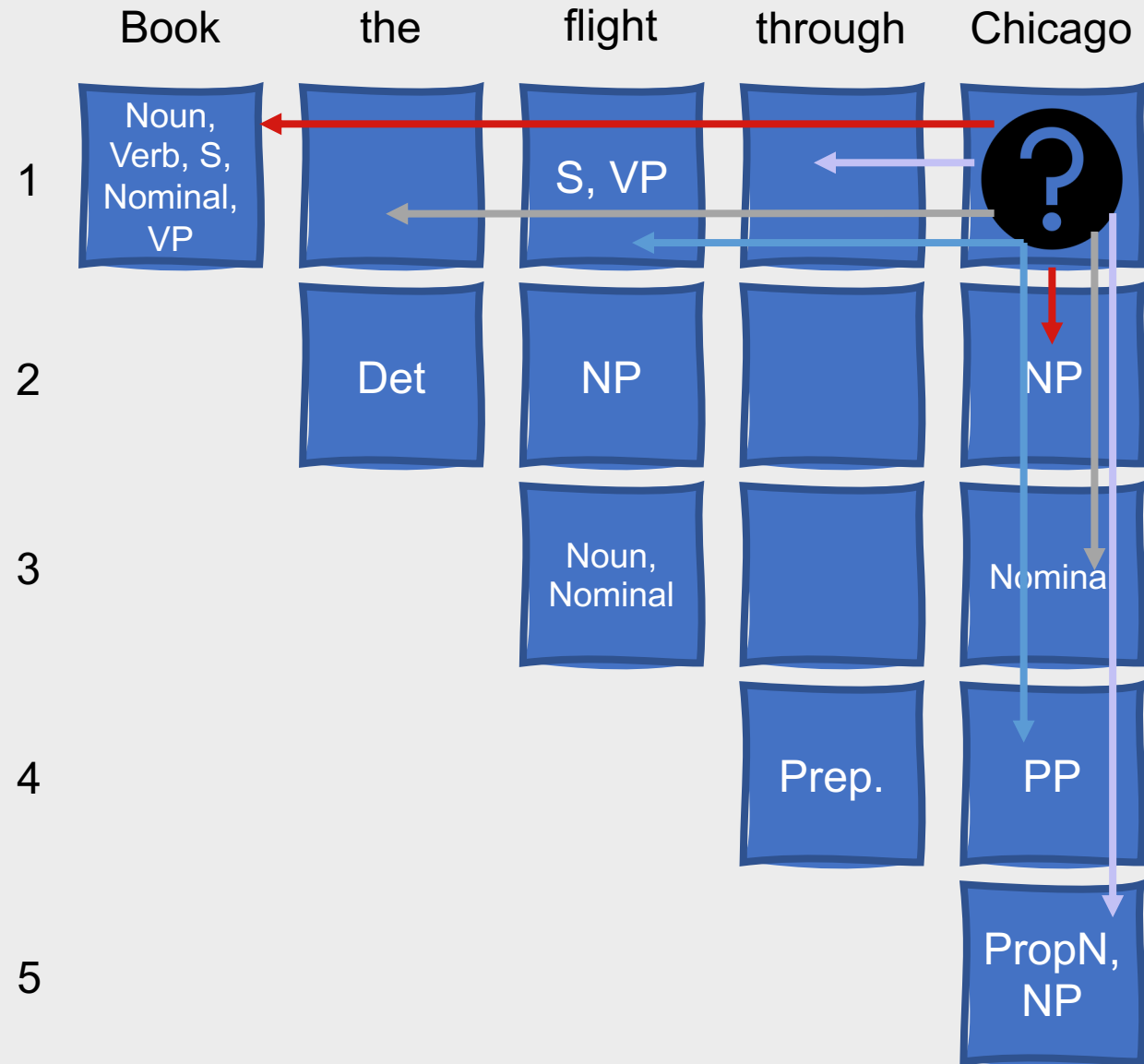




# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
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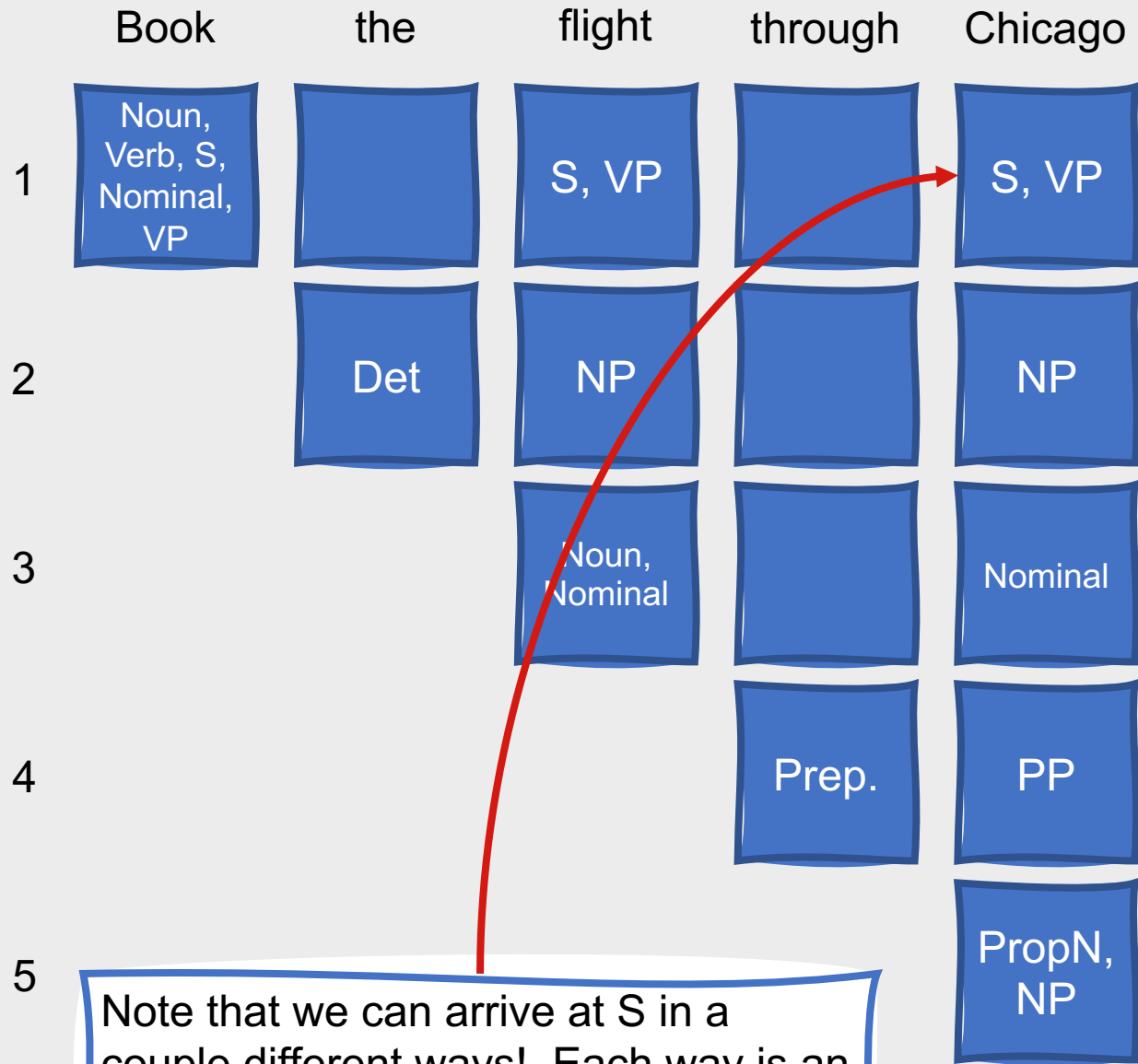
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 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP



# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

S → NP VP  
 S → **VP** → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → **Verb NP**  
 VP → Verb PP  
 VP → **VP PP**  
 PP → Preposition NP



Note that we can arrive at S in a couple different ways! Each way is an alternative parse.

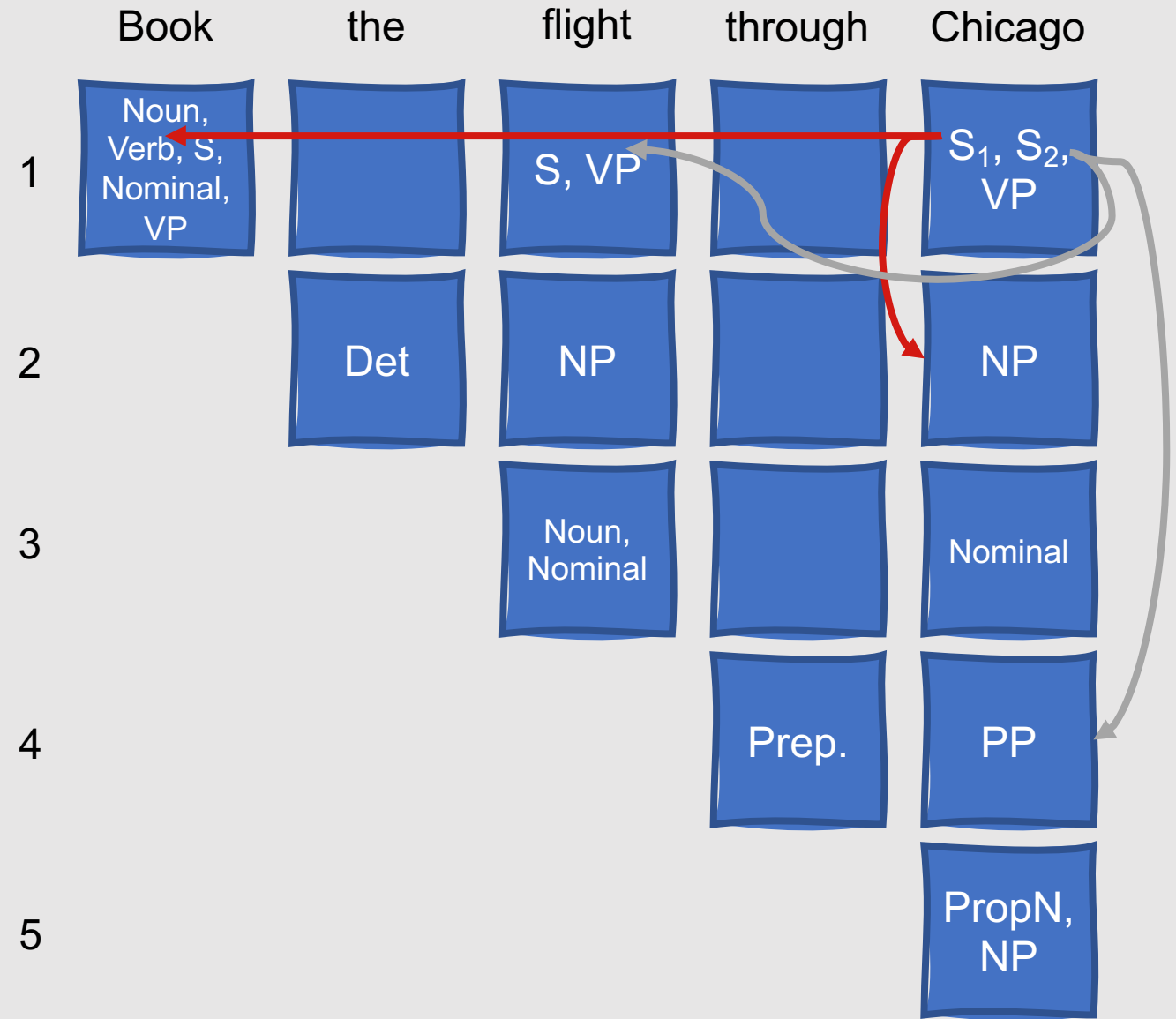
# CKY Algorithm

- The example we just saw functions as a **recognizer** ...for it to succeed (i.e., find a valid sentence according to this grammar), it simply needs to find an S in cell [0,n]
- To return all possible parses, we need to make two changes to the algorithm:
  - Pair each non-terminal with pointers to the table entries from which it was derived
  - Permit multiple versions of the same non-terminal to be entered into the table
- Then, we can choose an S from cell [0,n] and recursively retrieve its component constituents from the table

# CKY Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer  
 Pronoun → I | she | me  
 Proper-Noun → Chicago | Dallas  
 Aux → does  
 Preposition → from | to | on | near | through

S → NP VP  
 S → VP → Verb → book | include | prefer  
 NP → Pronoun → I | she | me  
 NP → Proper-Noun → Chicago | Dallas  
 NP → Det Nominal  
 Nominal → Noun → book | flight | meal | money  
 Nominal → Nominal Noun  
 Nominal → Nominal PP  
 VP → Verb → book | include | prefer  
 VP → Verb NP  
 VP → Verb PP  
 VP → VP PP  
 PP → Preposition NP





CKY  
Complexity

Time Complexity:  
 $O(n^3)$

Space Complexity:  
 $O(n^2)$

# How can we improve upon CKY?

- Fill table in a single sweep over the input words, using a top-down approach
- Table is length  $n+1$ , where  $n$  is equivalent to the number of words
- Table entries contain three types of information:
  - A subtree corresponding to a single grammar rule
  - Information about the progress made in completing the subtree
  - The position of the subtree with respect to the input
- This is called Earley parsing

In Earley  
parsing,  
table entries  
are known  
as states.

- States include structures called **dotted rules**
- A • within the righthand side of a state's grammar rule indicates the progress made towards recognizing it
- A state's **position with respect to the input is represented by two numbers**, indicating (1) where the state begins, and (2) where its dot lies

# Example States

- Input: Book that flight.
- $S \rightarrow \bullet VP, [0,0]$ 
  - Top-down prediction for this particular kind of S
  - First 0: Constituent predicted by this state should begin at the start of the input
  - Second 0: Dot lies at the start of the input as well
- $NP \rightarrow Det \bullet Nominal, [1,2]$ 
  - NP begins at position 1
  - Det has been successfully parsed
  - Nominal is expected next
- $VP \rightarrow V NP \bullet, [0,3]$ 
  - Successful discovery of a tree corresponding to a VP that spans the entire input



# Earley Algorithm

- An Earley parser moves through the  $n+1$  sets of states in a chart in a left-to-right fashion, processing the states within each set in order
- At each step, one of three operators is applied to each state depending on its status
  - Predictor
  - Scanner
  - Completer
- This results in the addition of new states to the end of either the current or next set of states in the chart
- States are never removed
- The algorithm never backtracks
- The presence of  $S \rightarrow \alpha \cdot$ ,  $[0, n]$  in the list of states in the last chart entry indicates a successful parse

# Earley Operators: Predictor

## Predictor

- Creates new states representing top-down expectations
- Applied to any state that has a non-terminal immediately to the right of its dot (as long as the non-terminal is not a POS category)
- New states are placed into the same chart entry as the generating state
- They begin and end at the same point in the input where the generating state ends

$S \rightarrow \cdot VP, [0,0]$

- $VP \rightarrow \cdot Verb, [0,0]$
- $VP \rightarrow \cdot Verb NP, [0,0]$
- $VP \rightarrow \cdot Verb NP PP, [0,0]$
- $VP \rightarrow \cdot Verb PP, [0,0]$
- $VP \rightarrow \cdot VP PP, [0,0]$

# Earley Operators: Scanner

- Used when a state has a POS category to the right of the dot
- Examines input and incorporates a state corresponding to the prediction of a word with a particular POS into the chart
- Does so by creating a new state from the input state with the dot advanced over the predicted input category
- $VP \rightarrow \bullet \text{ Verb NP}, [0,0]$ 
  - Since category following the dot is a part of speech (Verb)....
  - $\text{Verb} \rightarrow \text{book} \bullet, [0,1]$

# Earley Operators: Completer

- Applied to a state when its dot has reached the right end of the rule
- Indicates that the parser has successfully discovered a particular grammatical category over some span of input
- Purpose: Find and advance all previously created states that were looking for this grammatical category at this position in the input
- New states are created by copying the older state, advancing the dot over the expected category, and installing the new state in the current chart entry
- $NP \rightarrow \text{Det Nominal} \bullet$ , [1,3]
  - What incomplete states end at position 1 and expect an NP?
  - $VP \rightarrow \text{Verb} \bullet NP$ , [0,1]
  - $VP \rightarrow \text{Verb} \bullet NP PP$ , [0,1]
  - So, add  $VP \rightarrow \text{Verb NP} \bullet$ , [0,3] and the new incomplete  $VP \rightarrow \text{Verb NP} \bullet PP$ , [0,3] to the chart

# Earley Algorithm: Example

Chart	State	Rule	Start, End	Operator
0	S0	$\gamma \rightarrow \bullet S$	0, 0	Start State
0	S1	$S \rightarrow \bullet NP VP$	0, 0	Predictor
0	S2	$S \rightarrow \bullet VP$	0, 0	Predictor
0	S3	$NP \rightarrow \bullet Det Nominal$	0, 0	Predictor
0	S4	$VP \rightarrow \bullet Verb$	0, 0	Predictor
0	S5	$VP \rightarrow \bullet Verb NP$	0, 0	Predictor

Det  $\rightarrow$  that | this | a | the  
Noun  $\rightarrow$  book | flight | meal | money  
Verb  $\rightarrow$  book | include | prefer

S  $\rightarrow$  NP VP  
S  $\rightarrow$  VP  
NP  $\rightarrow$  Det Nominal  
Nominal  $\rightarrow$  Noun  
Nominal  $\rightarrow$  Nominal Noun  
VP  $\rightarrow$  Verb  
VP  $\rightarrow$  Verb NP

# Earley Algorithm: Example

Chart	State	Rule	Start, End	Operator
0	S0	$\gamma \rightarrow \bullet S$	0, 0	Start State
0	S1	$S \rightarrow \bullet NP VP$	0, 0	Predictor
0	S2	$S \rightarrow \bullet VP$	0, 0	Predictor
0	S3	$NP \rightarrow \bullet Det Nominal$	0, 0	Predictor
0	S4	$VP \rightarrow \bullet Verb$	0, 0	Predictor
0	S5	$VP \rightarrow \bullet Verb NP$	0, 0	Predictor
1	S6	$Verb \rightarrow book \bullet$	0, 1	Scanner
1	S7	$VP \rightarrow Verb \bullet$	0, 1	Completer
1	S8	$VP \rightarrow Verb \bullet NP$	0, 1	Completer
1	S9	$S \rightarrow VP \bullet$	0, 1	Completer
1	S10	$NP \rightarrow \bullet Det Nominal$	1, 1	Predictor

Det  $\rightarrow$  that | this | a | the  
 Noun  $\rightarrow$  book | flight | meal | money  
 Verb  $\rightarrow$  book | include | prefer

S  $\rightarrow$  NP VP  
 S  $\rightarrow$  VP  
 NP  $\rightarrow$  Det Nominal  
 Nominal  $\rightarrow$  Noun  
 Nominal  $\rightarrow$  Nominal Noun  
 VP  $\rightarrow$  Verb  
 VP  $\rightarrow$  Verb NP

# Earley Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer

S → NP VP  
 S → VP  
 NP → Det Nominal  
 Nominal → Noun  
 Nominal → Nominal Noun  
 VP → Verb  
 VP → Verb NP

Chart	State	Rule	Start, End	Operator
0	S0	$\gamma \rightarrow \bullet S$	0, 0	Start State
0	S1	$S \rightarrow \bullet NP VP$	0, 0	Predictor
0	S2	$S \rightarrow \bullet VP$	0, 0	Predictor
0	S3	$NP \rightarrow \bullet Det Nominal$	0, 0	Predictor
0	S4	$VP \rightarrow \bullet Verb$	0, 0	Predictor
0	S5	$VP \rightarrow \bullet Verb NP$	0, 0	Predictor
1	S6	$Verb \rightarrow book \bullet$	0, 1	Scanner
1	S7	$VP \rightarrow Verb \bullet$	0, 1	Completer
1	S8	$VP \rightarrow Verb \bullet NP$	0, 1	Completer
1	S9	$S \rightarrow VP \bullet$	0, 1	Completer
1	S10	$NP \rightarrow \bullet Det Nominal$	1, 1	Predictor
2	S11	$Det \rightarrow that \bullet$	1, 2	Scanner
2	S12	$NP \rightarrow Det \bullet Nominal$	1, 2	Completer
2	S13	$Nominal \rightarrow \bullet Noun$	2, 2	Predictor
2	S14	$Nominal \rightarrow \bullet Nominal Noun$	2, 2	Predictor

# Earley Algorithm: Example

Det → that | this | a | the  
 Noun → book | flight | meal | money  
 Verb → book | include | prefer

S → NP VP  
 S → VP  
 NP → Det Nominal  
 Nominal → Noun  
 Nominal → Nominal Noun  
 VP → Verb  
 VP → Verb NP

Chart	State	Rule	Start, End	Operator
0	S0	$\gamma \rightarrow \bullet S$	0, 0	Start State
0	S1	$S \rightarrow \bullet NP VP$	0, 0	Predictor
0	S2	$S \rightarrow \bullet VP$	0, 0	Predictor
0	S3	$NP \rightarrow \bullet Det Nominal$	0, 0	Predictor
0	S4	$VP \rightarrow \bullet Verb$	0, 0	Predictor
0	S5	$VP \rightarrow \bullet Verb NP$	0, 0	Predictor
1	S6	$Verb \rightarrow book \bullet$	0, 1	Scanner
1	S7	$VP \rightarrow Verb \bullet$	0, 1	Completer
1	S8	$VP \rightarrow Verb \bullet NP$	0, 1	Completer
1	S9	$S \rightarrow VP \bullet$	0, 1	Completer
1	S10	$NP \rightarrow \bullet Det Nominal$	1, 1	Predictor
2	S11	$Det \rightarrow that \bullet$	1, 2	Scanner
2	S12	$NP \rightarrow Det \bullet Nominal$	1, 2	Completer
2	S13	$Nominal \rightarrow \bullet Noun$	2, 2	Predictor
2	S14	$Nominal \rightarrow \bullet Nominal Noun$	2, 2	Predictor
3	S15	$Noun \rightarrow flight \bullet$	2, 3	Scanner
3	S16	$Nominal \rightarrow Noun \bullet$	2, 3	Completer
3	S17	$NP \rightarrow Det Nominal \bullet$	1, 3	Completer
3	S18	$Nominal \rightarrow Nominal \bullet Noun$	2, 3	Completer
3	S19	$VP \rightarrow Verb NP \bullet$	0, 3	Completer
3	S20	$S \rightarrow VP \bullet$	0, 3	Completer



# Which states participate in the final parse?

Chart	State	Rule	Start, End	Operator
0	S0	$\gamma \rightarrow \bullet S$	0, 0	Start State
0	S1	$S \rightarrow \bullet NP VP$	0, 0	Predictor
0	S2	$S \rightarrow \bullet VP$	0, 0	Predictor
0	S3	$NP \rightarrow \bullet Det Nominal$	0, 0	Predictor
0	S4	$VP \rightarrow \bullet Verb$	0, 0	Predictor
0	S5	$VP \rightarrow \bullet Verb NP$	0, 0	Predictor
1	S6	$Verb \rightarrow book \bullet$	0, 1	Scanner
1	S7	$VP \rightarrow Verb \bullet$	0, 1	Completer
1	S8	$VP \rightarrow Verb \bullet NP$	0, 1	Completer
1	S9	$S \rightarrow VP \bullet$	0, 1	Completer
1	S10	$NP \rightarrow \bullet Det Nominal$	1, 1	Predictor
2	S11	$Det \rightarrow that \bullet$	1, 2	Scanner
2	S12	$NP \rightarrow Det \bullet Nominal$	1, 2	Completer
2	S13	$Nominal \rightarrow \bullet Noun$	2, 2	Predictor
2	S14	$Nominal \rightarrow \bullet Nominal Noun$	2, 2	Predictor
3	S15	$Noun \rightarrow flight \bullet$	2, 3	Scanner
3	S16	$Nominal \rightarrow Noun \bullet$	2, 3	Completer
3	S17	$NP \rightarrow Det Nominal \bullet$	1, 3	Completer
3	S18	$Nominal \rightarrow Nominal \bullet Noun$	2, 3	Completer
3	S19	$VP \rightarrow Verb NP \bullet$	0, 3	Completer
3	S20	$S \rightarrow VP \bullet$	0, 3	Completer

**As with  
CKY, the  
example  
algorithm  
acted as a  
recognizer.**

- We can retrieve parse trees by adding a field to store information about the completed states that generated constituents
- How to do this?
  - Have the Completer operator add a pointer to the previous state onto a list of constituent states for the new state
  - When an S is found in the final chart, just follow pointers backward

# Which states participate in the final parse?

Chart	State	Rule	Start, End	Operator (Backward Pointer)
0	S0	$\gamma \rightarrow \bullet S$	0, 0	Start State
0	S1	$S \rightarrow \bullet NP VP$	0, 0	Predictor
0	S2	$S \rightarrow \bullet VP$	0, 0	Predictor
0	S3	$NP \rightarrow \bullet Det Nominal$	0, 0	Predictor
0	S4	$VP \rightarrow \bullet Verb$	0, 0	Predictor
0	S5	$VP \rightarrow \bullet Verb NP$	0, 0	Predictor
1	S6	$Verb \rightarrow book \bullet$	0, 1	Scanner
1	S7	$VP \rightarrow Verb \bullet$	0, 1	Completer
1	S8	$VP \rightarrow Verb \bullet NP$	0, 1	Completer
1	S9	$S \rightarrow VP \bullet$	0, 1	Completer
1	S10	$NP \rightarrow \bullet Det Nominal$	1, 1	Predictor
2	S11	$Det \rightarrow that \bullet$	1, 2	Scanner
2	S12	$NP \rightarrow Det \bullet Nominal$	1, 2	Completer
2	S13	$Nominal \rightarrow \bullet Noun$	2, 2	Predictor
2	S14	$Nominal \rightarrow \bullet Nominal Noun$	2, 2	Predictor
3	S15	$Noun \rightarrow flight \bullet$	2, 3	Scanner
3	S16	$Nominal \rightarrow Noun \bullet$	2, 3	Completer (S15)
3	S17	$NP \rightarrow Det Nominal \bullet$	1, 3	Completer (S11, S15)
3	S18	$Nominal \rightarrow Nominal \bullet Noun$	2, 3	Completer
3	S19	$VP \rightarrow Verb NP \bullet$	0, 3	Completer (S6, S17)
3	S20	$S \rightarrow VP \bullet$	0, 3	Completer (S19)

# Summary: Syntactic Parsing

- **Syntactic parsing** is the process of automatically determining the grammatical structure of an input sentence
- Language is ambiguous, so **sentences can have multiple grammatically-correct parses**
- Parsing can be performed using either a **top-down** or **bottom-up** approach
- Common algorithms for syntactic parsing include:
  - **CKY**
  - **Earley**

# What is dependency parsing?

- Automatically determining **directed grammatical (and semantic!) relationships** between words in a sentence.
  - **Syntactic**: Focused on **sentence structure**
  - **Semantic**: Focused on **meaning**

How are dependency grammars different from CFGs?

- CFGs are used to automatically generate constituent-based representations
  - Noun phrases, verb phrases, etc.
- Dependency grammars ignore phrase-structure rules, and instead define sentence structure in terms of the relationships between individual words
  - Nominal subject, direct object, etc.
- For both, labels are still drawn from a fixed inventory of grammatical relations

Dependency grammars can deal with languages that are **morphologically rich** and have a **relatively free word order**.

---

**Morphologically rich:** More inflections (changes to words that influence meaning or grammatical relation)

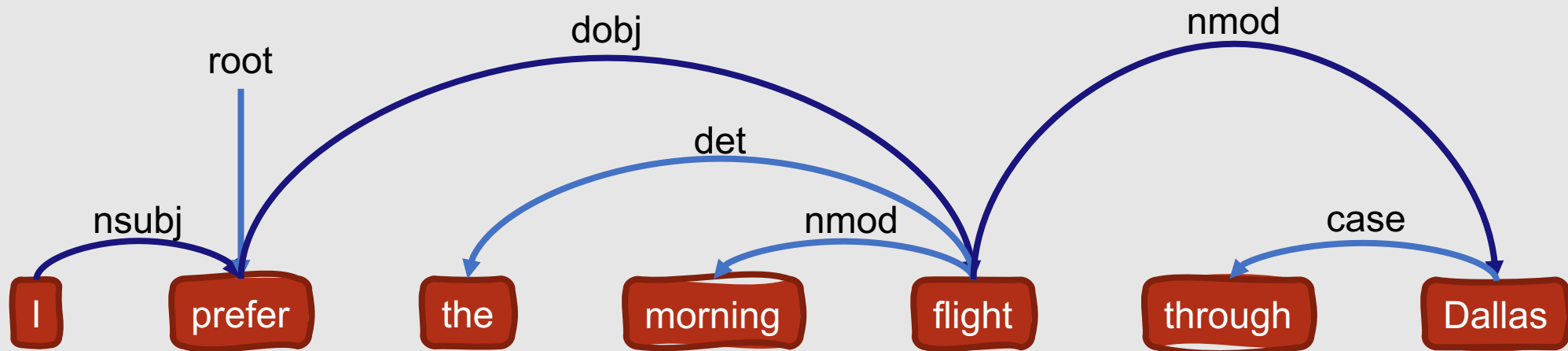
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**Free word order:** Words can be moved around in a sentence but the overall meaning will remain the same (syntax is less important)

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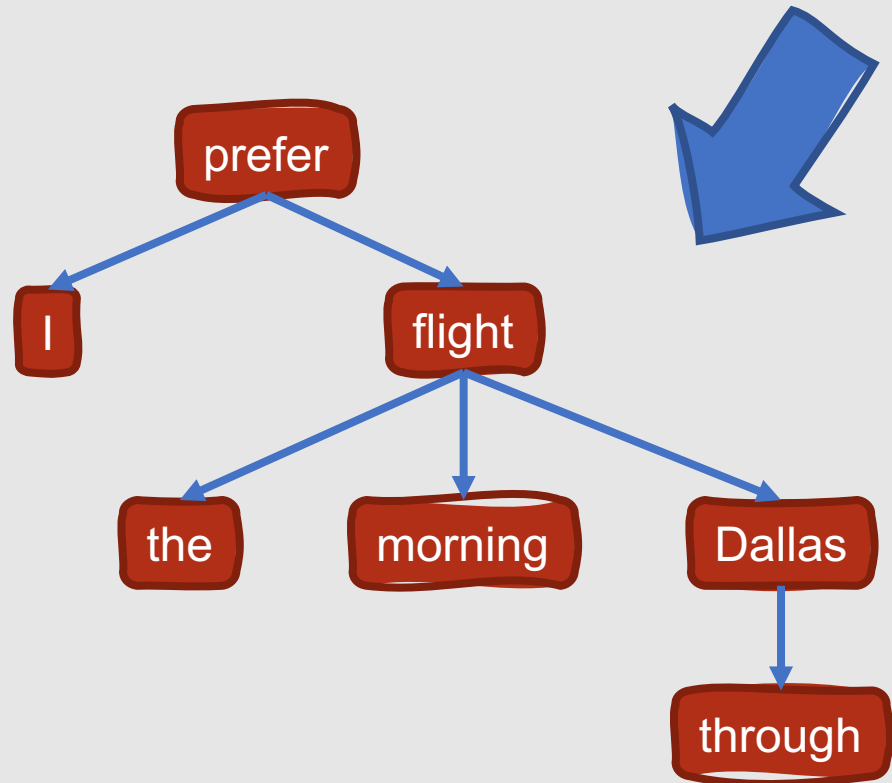
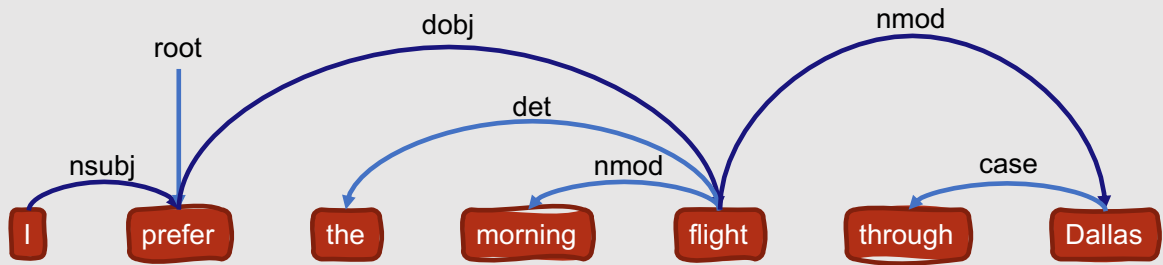
Typically, there is a trade-off between morphological richness and importance of syntax

# Typed Dependency Structure

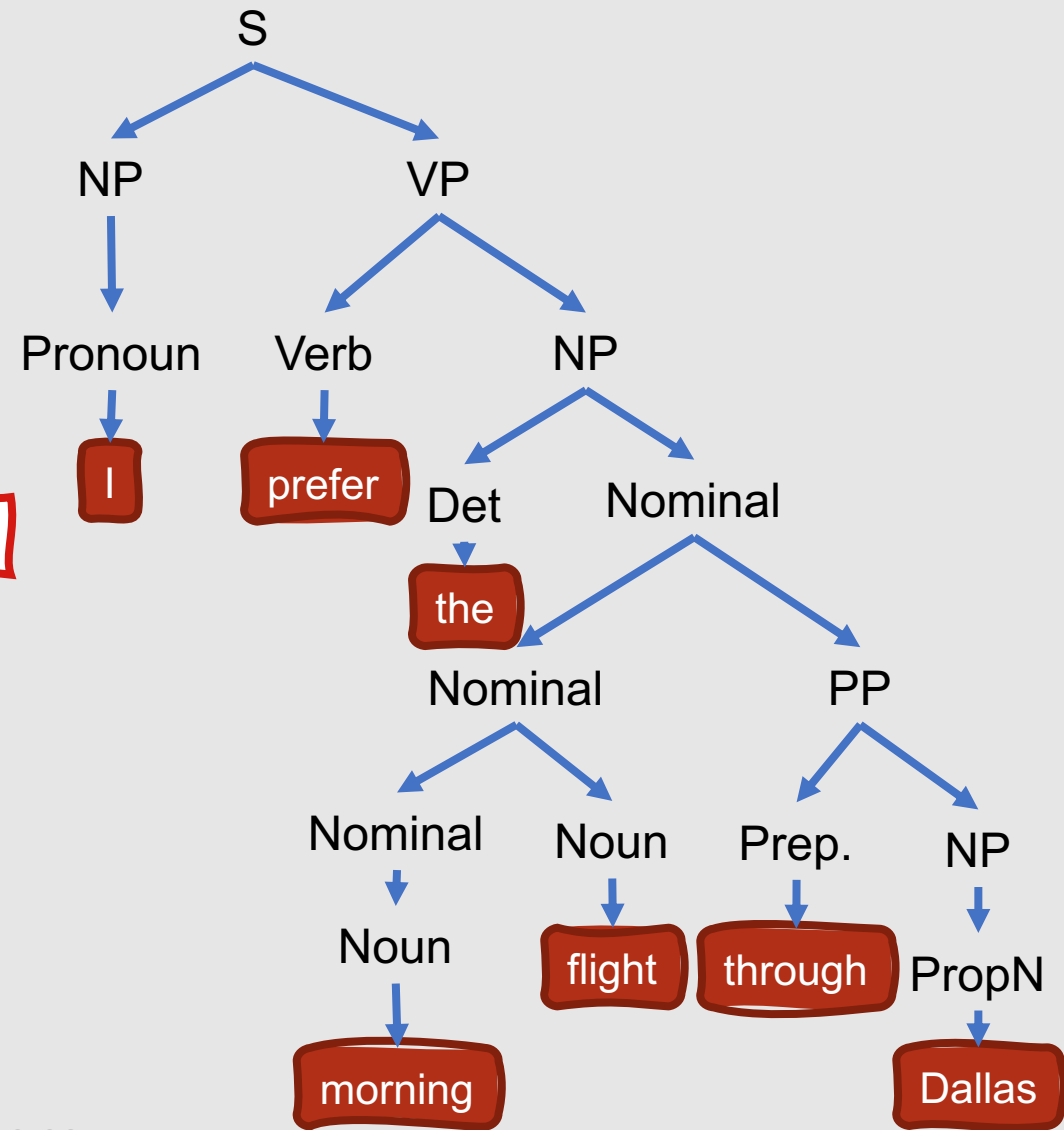




# Comparison with Syntactic Parse



vs.



## Why is dependency parsing useful?

- Dependency parsing provides an approximation of the semantic relationships between different words in a sentence and their arguments
- This information is useful for many NLP applications, including:
  - Coreference resolution
  - Question answering
  - Information extraction

# Dependency Relations

- Two components:
  - **Head**
  - **Dependent**
- **Heads** are linked to the words that are immediately **dependent** on them
- Relation types describe the **dependent's** role with respect to its **head**
  - Subject
  - Direct object
  - Indirect object

# Dependency Relations

- Relation types tend to correlate with sentence position and constituent type in English, but there is not an explicit connection between these elements
- In more flexible languages (e.g., those with relatively free word order), the information encoded in these relation types often cannot be estimated otherwise (e.g., by using a constituent tree)

**Just like with CFGs, there are a variety of taxonomies that can be used to label dependencies between words.**

These are often referred to as dependency treebanks

A few of the most popular dependency treebanks include:

- Stanford dependencies
- CoNLL dependencies
- Universal dependencies

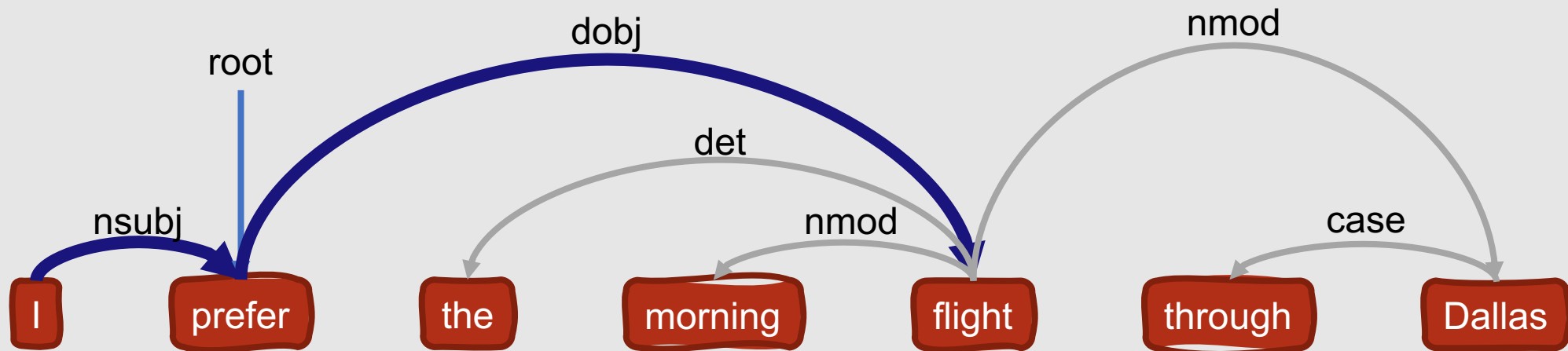
Just like with other corpora we've discussed so far, these treebanks are typically created by either:

- Having human annotators manually create dependency structures for a collection of sentences
- Automatically creating initial dependency structures and then having human annotators manually correct those structures

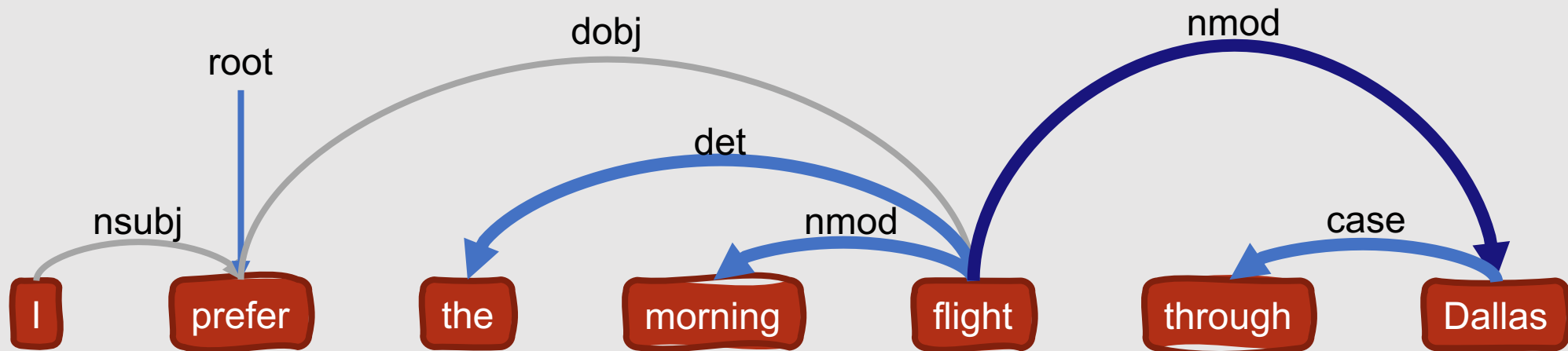
Recently, most  
researchers  
have moved  
toward using  
universal  
dependencies.

- Universal dependencies can be broken into two sets
  - **Clausal Relations:** Describe syntactic roles with respect to predicates (the part(s) of the sentence that say something about the subject)
  - **Modifier Relations:** Describe the ways that words can modify their heads

# Clausal Relations



# Modifier Relations





# Universal Dependencies

Structural categories of dependent

	Nominals	Clauses	Modifier Words	Function Words
Core Arguments of Clausal Predicates	nsubj obj iobj	csubj ccomp xcomp		
Non-Core Dependents of Clausal Predicates	obl vocative expl dislocated	advcl	advmod discourse	aux cop mark
Dependents of Nominals	nmod appos nummod	acl	amod	det case

Functional categories w.r.t. head

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details):  
conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep

# Universal Dependencies

Structural categories of dependent

		Nominals	Clauses	Modifier Words	Function Words
Functional categories w.r.t. head	Core Arguments of Clausal Predicates	nsubj obj iobj	<div style="border: 2px solid red; padding: 5px;">                     Natalie wrote a dissertation.  <b>nsubj(wrote, Natalie)</b> </div>		
	Non-Core Dependents of Clausal Predicates	obl vocative expl dislocated	<div style="border: 2px solid red; padding: 5px;">                     Natalie wrote a dissertation.  <b>obj(wrote, dissertation)</b> </div>		aux cop mark
	Dependents of Nominals	nmod appos nummod	<div style="border: 2px solid red; padding: 5px;">                     Natalie wrote him a dissertation.  <b>iobj(wrote, him)</b> </div>		det case

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details): conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep

# Universal Dependencies

Structural categories of dependent

		Structural categories of dependent			
		Nominals	Clauses	Modifier Words	Function Words
Functional categories w.r.t. head	Core Arguments of Clausal Predicates	nsubj obj iobj	<div style="border: 2px solid red; padding: 5px;">                     Natalie wrote a dissertation for him.  <b>obl(wrote, him)</b> </div>		
	Non-Core Dependents of Clausal Predicates	obl vocative expl dislocated	<div style="border: 2px solid red; padding: 5px;">                     Natalie, read my dissertation!  <b>vocative(read, Natalie)</b> </div>		aux cop mark
	Dependents of Nominals	nmod appos nummod	<div style="border: 2px solid red; padding: 5px;">                     It is clear that her dissertation is a masterpiece.  <b>expl(clear, it)</b> </div>		et case
			<div style="border: 2px solid red; padding: 5px;">                     You must not eat it, the dissertation.  <b>dislocated(eat, dissertation)</b> </div>		

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details): conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep

# Universal Dependencies

Structural categories of dependent

		Nominals	Clauses	Modifier Words	Function Words
Functional categories w.r.t. head	Core Arguments of Clausal Predicates	nsubj obj iobj	The purpose of this dissertation is to determine an optimal strategy for selecting fantasy football teams. <b>nmod(purpose, dissertation)</b>		
	Non-Core Dependents of Clausal Predicates	obl vocative expl dislocated	My advisor, Natalie, is boring me. <b>appos(advisor, Natalie)</b>		aux cop mark
	Dependents of Nominals	nmod appos nummod	Yesterday she wrote five dissertations. <b>nummod(dissertations, five)</b>		det case

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details):  
conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep

# Universal Dependencies

Structural categories of dependent

		Structural categories of dependent			
		Nominals	Clauses	Modifier Words	Function Words
Functional categories w.r.t. head	<b>Core Arguments of Clausal Predicates</b>	nsubj obj iobj	<b>csubj</b> ccomp xcomp		
	<b>Non-Core Dependents of Clausal Predicates</b>	obl vocative expl dislocated	advcl		aux
	<b>Dependents of Nominals</b>	nmod appos nummod	acl		det

What she said about only choosing fantasy football players from northern teams makes sense.  
**csubj(makes, said)**

She said to read her second dissertation for more tips.  
**ccomp(said, read)**

I consider her a genius.  
**xcomp(consider, genius)**

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details): conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep

# Universal Dependencies

Structural categories of dependent

		Structural categories of dependent			
		Nominals	Clauses	Modifier Words	Function Words
Functional categories w.r.t. head	<b>Core Arguments of Clausal Predicates</b>	nsubj obj iobj	csubj ccomp xcomp	<div style="border: 2px solid red; padding: 5px;">                     He was upset when she read her dissertation to him.  <b>advcl(upset, read)</b> </div>	
	<b>Non-Core Dependents of Clausal Predicates</b>	obl vocative expl dislocated	advcl		
	<b>Dependents of Nominals</b>	nmod appos nummod	acl	amod	det case

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details): conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep

# Universal Dependencies

Structural categories of dependent

Functional categories w.r.t. head	Nominals	Clauses	Modifier Words	Function Words	
	Core Arguments of Clausal Predicates	nsubj obj iobj	csubj ccomp xcomp		
	Non-Core Dependents of Clausal Predicates	obl vocative expl dislocated	advcl		
	Dependents of Nominals	nmod appos nummod	acl	amod	det case

She added an appendix discussing fantasy bachelor.  
**acl(appendix, discussing)**

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details):  
 conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep

# Universal Dependencies

Structural categories of dependent

		Nominals	Clauses	Modifier Words	Function Words
Functional categories w.r.t. head	Core Arguments of Clausal Predicates	<div style="border: 2px solid red; padding: 5px;">                     He was deeply offended by the generalization from football to reality show.  <b>advmod(offended, deeply)</b> </div>			
	Non-Core Dependents of Clausal Predicates	obl vocative expl dislocated	advcl	advmod discourse	aux cop mark
	Dependents of Nominals				det case

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details): conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep



# Universal Dependencies

Structural categories of dependent

		Structural categories of dependent			
		Nominals	Clauses	Modifier Words	Function Words
Functional categories w.r.t. head	Core Arguments of Clausal Predicates	nsubj obj iobj	csubj ccomp xcomp		
	Non-Core Dependents of Clausal Predicates	<div style="border: 2px solid red; padding: 5px;">                     He sat with rapt attention as she began reading an excerpt from her third dissertation.  <b>amod(attention, rapt)</b> </div>		advmod discourse	aux cop mark
	Dependents of Nominals			nmod appos nummod	acl

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details): conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep

# Universal Dependencies

Structural categories of dependent

		Nominals	Clauses	Modifier Words	Function Words
Functional categories w.r.t. head	Core Arguments of Clausal Predicates	<div style="border: 2px solid red; padding: 5px;">                     She had included case studies.  <b>aux(included, had)</b> </div>			
	Non-Core Dependents of Clausal Predicates	<div style="border: 2px solid red; padding: 5px;">                     The studies demonstrated that both fantasy games were essentially the same.  <b>cop(same, were)</b> </div>			aux cop mark
	Dependents of Nominals	<div style="border: 2px solid red; padding: 5px;">                     He knew that this would change life as he knew it.  <b>mark(change, that)</b> </div>			det case

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details): conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep

# Universal Dependencies

		Structural categories of dependent			
		Nominals	Clauses	Modifier Words	Function Words
Functional categories w.r.t. head	Core Arguments of Clausal Predicates	nsubj obj iobj	<div style="border: 2px solid red; padding: 5px;">                     She told him that was the point.  <b>det(point, the)</b> </div>		
	Non-Core Dependents of Clausal Predicates	obl vocative	advcl	advmod discourse	aux cop mark
	Dependents of Nominals	nmod appos nummod	acl	amod	det case

Other miscellaneous dependency relations (see <https://universaldependencies.org/u/dep/index.html> for details): conj, cc, fixed, flat, compound, list, parataxis, orphan, goeswith, reparandum, punct, root, dep

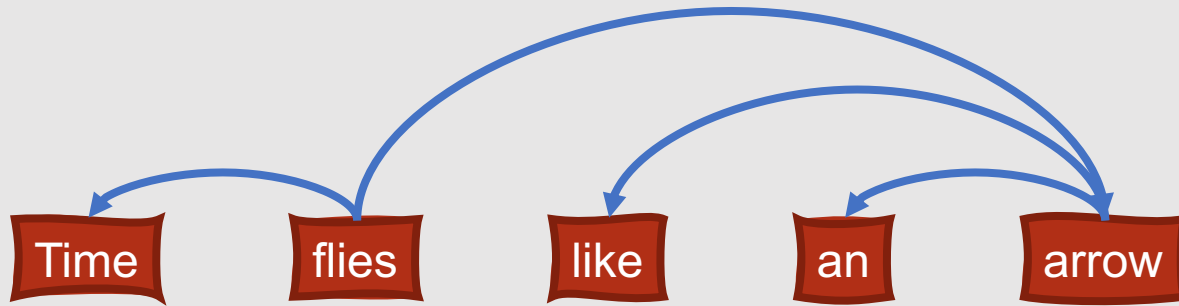
# In-Class Exercise

- Assign universal dependency relations to the following sentences:
  - **Time flies like an arrow.**
  - **Fruit flies like a banana.**

<https://www.google.com/search?q=timer>

	Nominals	Clauses	Modifier Words	Function Words
Core Arguments of Clausal Predicates	nsubj obj iobj	csubj ccomp xcomp		
Non-Core Dependents of Clausal Predicates	obl vocative expl dislocated	advcl	advmod discourse	aux cop mark
Dependents of Nominals	nmod appos nummod	acl	amod	det case

# In-Class Exercise



Fruit flies like a banana

nsubj

nmod

case

det

compound

obj

# Dependency Formalisms

- Dependency structures are directed graphs
  - $G = (V, A)$ 
    - $V$  is a set of vertices
    - $A$  is a set of ordered pairs of vertices, or arcs
  - $V$  corresponds to the words in a sentence
    - May also include punctuation
    - In morphologically complex languages, may include stems and affixes
  - Arcs capture the grammatical relationships between those words
- According to most grammatical theories (including those followed in this course), dependency structures:
  - Must be connected
  - Must have a designated root node
  - Must be acyclic

# Dependency Trees

- Directed graphs (such as those we've seen already) that satisfy the following constraints:
  - Single designated root node
    - No incoming arcs to the root!
  - All vertices *except the root node* have exactly one incoming arc
  - There is a unique path from the root node to each vertex

# How to translate from constituent to dependency structures?

## Two steps:

- Identify all head-dependent relations in the constituent tree
- Identify the correct dependency relations for those relations

## One algorithm for doing this:

- Mark the **head child** of each node in a phrase structure, based on a set of predetermined rules
- In the dependency structure, make the head of each **non-head child** depend on the head of the **head child**



However,  
doing this  
can  
produce  
results that  
are far from  
perfect!

- Most noun phrases do not have much (or any) internal structure
- Morphological information has little to no presence in phrase structure trees
- For **low resource languages** in particular, most dependency treebanks are developed manually by human annotators rather than attempting to automatically translate from constituent to dependency parse

# Types of Dependency Parsers

## Transition

### Transition-based

- Build a single tree in a left-to-right (assuming a left-to-right language) sweep over the input sentence

## Graph

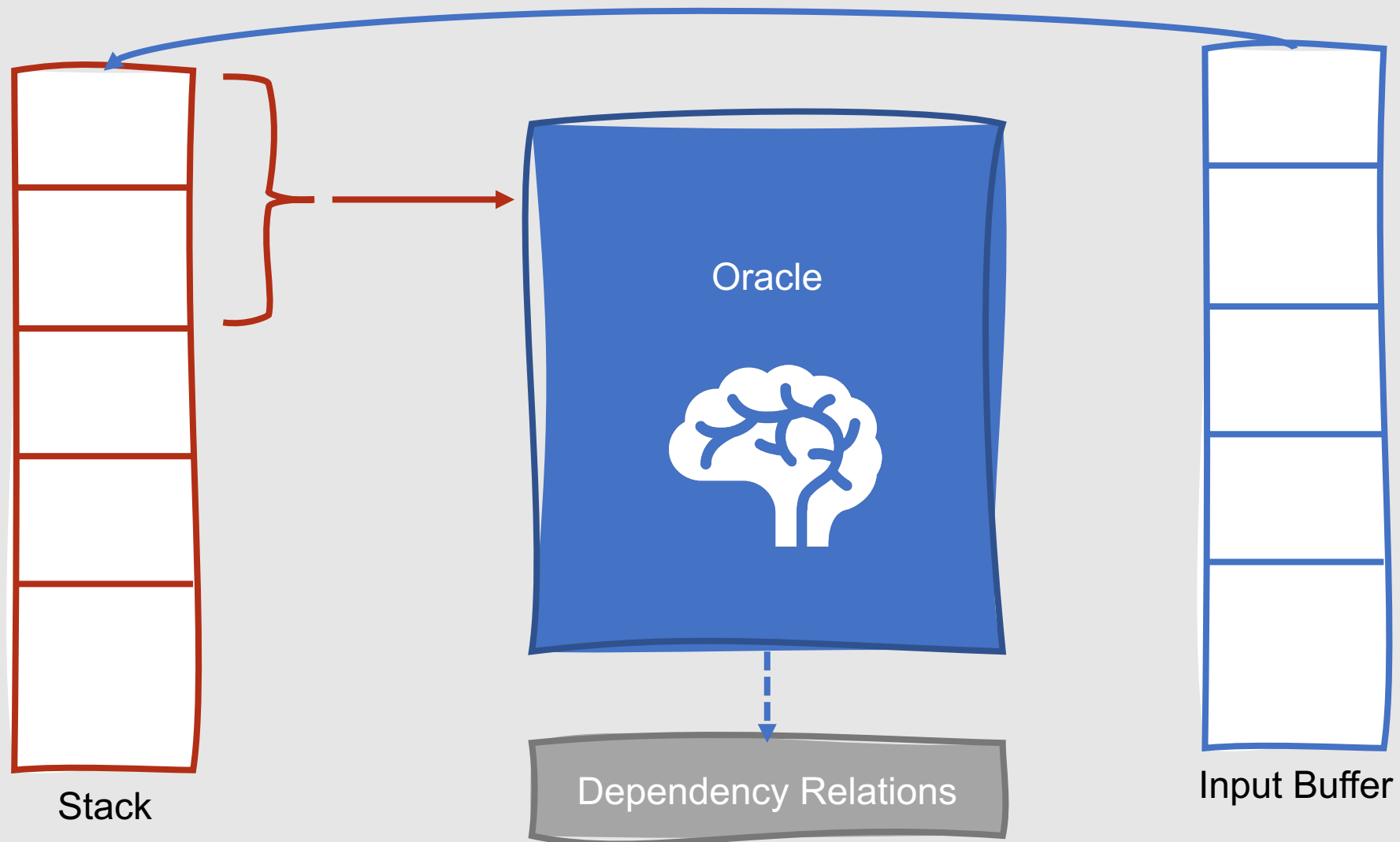
### Graph-based

- Search through the space of possible trees for a given sentence, and try to find the tree that maximizes some score

## Transition-based Dependency Parsing

- Earliest transition-based approach: **shift-reduce parsing**
  - Input tokens are successively shifted onto a stack
  - The two top elements of the stack are matched against a set of possible relations provided by some knowledge source
  - When a match is found, a head-dependent relation between the matched elements is asserted
- Goal is to find a final parse that accounts for all words

# Shift-Reduce Parsing



## Transition-based Parsing

- We can build upon shift-reduce parsing by defining a set of **transition operators** to guide the parser's decisions
- Transition operators work by producing new **configurations**:
  - Stack
  - Input buffer of words
  - Set of relations representing a dependency tree

# Transition- based Parsing

## Initial configuration:

- Stack contains the ROOT node
- Word list is initialized with all words in the sentence, in order
- Empty set of relations represents the parse

## Final configuration:

- Stack should be empty
- Word list should be empty
- Set of relations represents the parse

# Operators

- The operators used in transition-based parsing then perform the following tasks:
  - Assign the current word as the head of some other word that has already been seen
  - Assign some other word that has already been seen as the head of the current word
  - Do nothing with the current word

# Operators

- More formally, these operators are defined as:
  - **LeftArc**: Asserts a head-dependent relation between the word at the top of the stack and the word directly beneath it (the second word), and removes the second word from the stack
    - Cannot be applied when ROOT is the second element in the stack
    - Requires two elements on the stack
  - **RightArc**: Asserts a head-dependent relation between the second word and the word at the top of the stack, and removes the word at the top of the stack
    - Requires two elements on the stack
  - **Shift**: Removes a word from the front of the input buffer and pushes it onto the stack
- These operators implement the **arc standard approach** to transition-based parsing



# Arc Standard Approach to Transition- based Parsing

## Notable characteristics:

- Transition operators only assert relations between elements at the top of the stack
- Once an element has been assigned its head, it is removed from the stack
  - Not available for further processing!

## Benefits:

- Reasonably effective
- Simple to implement

# Formal Algorithm: Arc Standard Approach

```
state ← {[root], [words], []}
while state not final:
    # Choose which transition operator to apply
    transition ← oracle(state)

    # Apply the operator and create a new state
    state ← apply(transition, state)
```

# When does the process end?

- When all words in the sentence have been consumed
- When the ROOT node is the only element remaining on the stack

# Is this another example of dynamic programming?

- No! 😬
- The arc standard approach is a **greedy algorithm**
  - Oracle provides a single choice at each step
  - Parser proceeds with that choice
    - No other options explored
    - No backtracking
  - Single parse returned at the end

# Arc Standard: Example

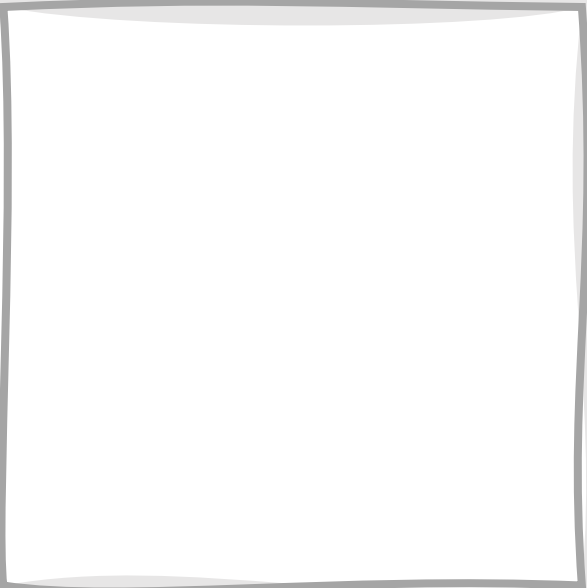
Input Buffer

book	me	the	morning	flight
------	----	-----	---------	--------

Stack

root					
------	--	--	--	--	--

Relations



# Arc Standard: Example

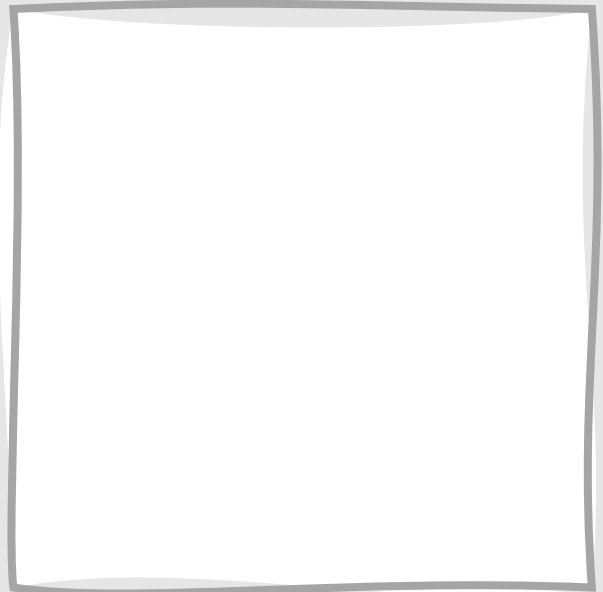
Input Buffer



Stack



Relations



Only one item in the stack!  
Shift **book** from the input buffer to the stack

# Arc Standard: Example

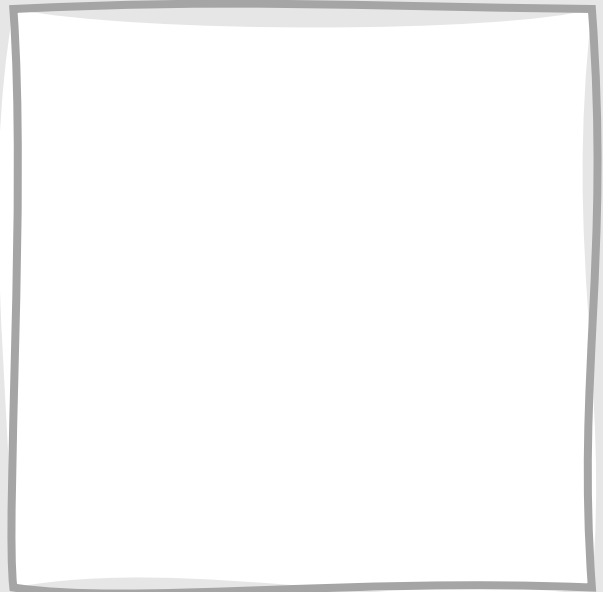
Input Buffer



Stack



Relations



Valid options: Shift, RightArc  
Oracle selects Shift  
Shift **me** from the input buffer to the stack

# Arc Standard: Example

Input Buffer

		the	morning	flight
--	--	-----	---------	--------

Stack

book	root				
------	------	--	--	--	--

Relations

(book → me)

Valid options: Shift,  
RightArc, LeftArc

Oracle selects RightArc

Remove **me** from the stack

Add relation (book → me) to  
the set of relations



# Arc Standard: Example

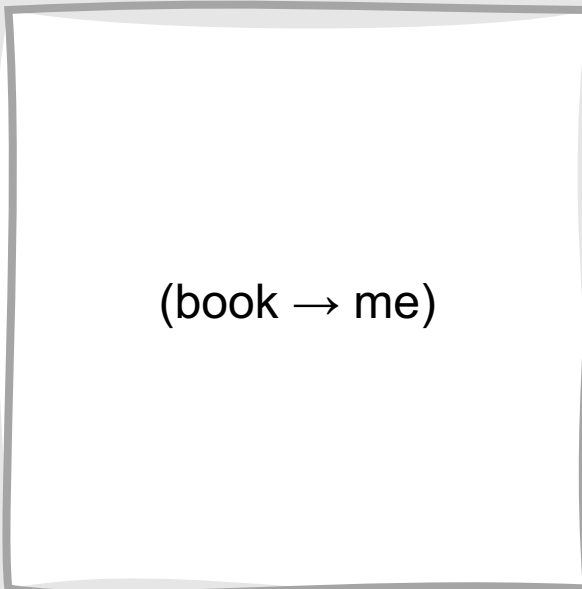
Input Buffer



Stack



Relations



Valid options: Shift, RightArc

Oracle selects Shift

Shift **the** from the input buffer to the stack

# Arc Standard: Example

Input Buffer 

Stack 

Relations

(book → me)

Valid options: Shift,  
RightArc, LeftArc

Oracle selects Shift

Shift **morning** from the input  
buffer to the stack

# Arc Standard: Example

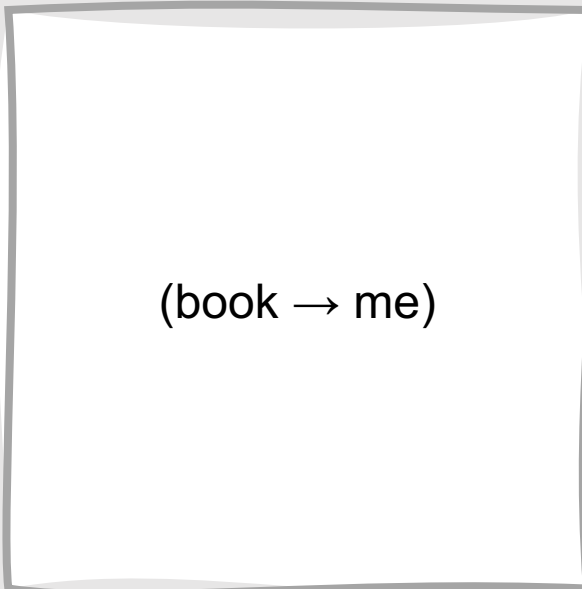
Input Buffer



Stack



Relations



Valid options: Shift,  
RightArc, LeftArc

Oracle selects Shift

Shift **flight** from the input  
buffer to the stack

# Arc Standard: Example

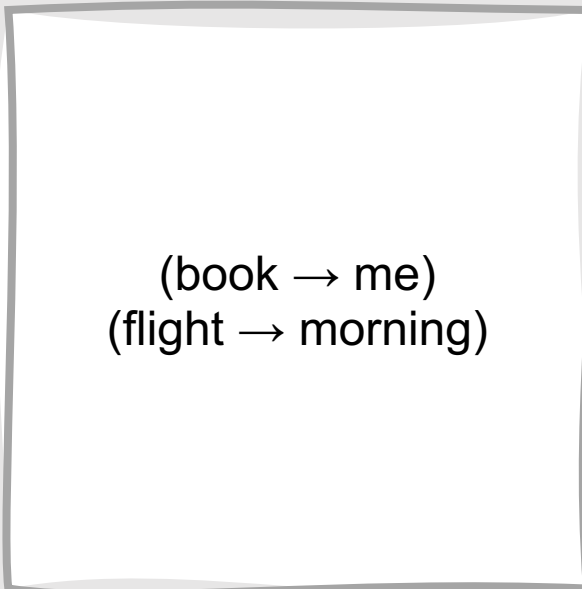
Input Buffer



Stack



Relations



Valid options: RightArc,  
LeftArc

Oracle selects LeftArc

Remove **morning** from the  
stack

Add relation (flight →  
morning) to the set of  
relations

# Arc Standard: Example

Input Buffer



Stack



Relations



Valid options: RightArc,  
LeftArc

Oracle selects LeftArc

Remove **the** from the stack

Add relation (flight → the) to  
the set of relations

# Arc Standard: Example

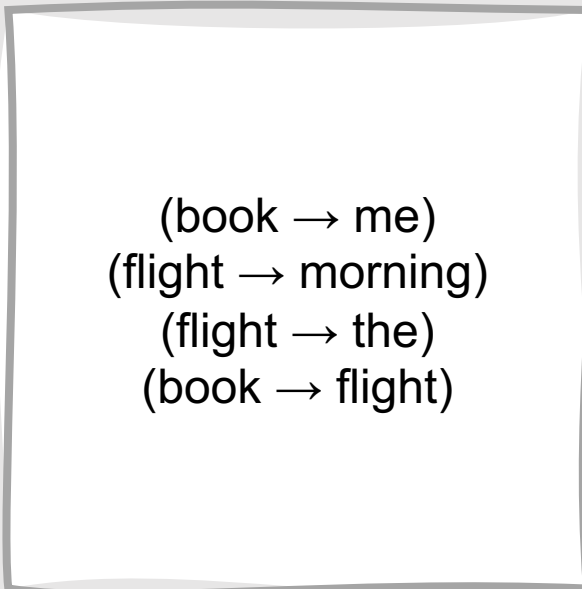
Input Buffer



Stack



Relations



Valid options: RightArc,  
LeftArc

Oracle selects RightArc

Remove **flight** from the  
stack

Add relation (book → flight)  
to the set of relations

# Arc Standard: Example

Input Buffer



Stack



Relations

(book → me)  
(flight → morning)  
(flight → the)  
(book → flight)  
(root → book)

Valid options: RightArc

Oracle selects RightArc

Remove **book** from the stack

Add relation (root → book) to the set of relations

# Arc Standard: Example

Input Buffer



Stack

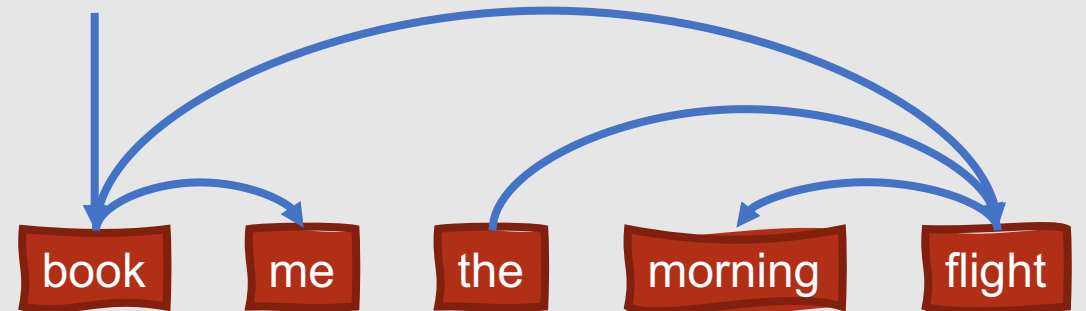


Valid options: None

State is final

Relations

(book → me)  
(flight → morning)  
(flight → the)  
(book → flight)  
(root → book)





# A few things worth noting....

- We assumed in the previous example that our oracle was always correct ...this is not necessarily (or perhaps not even likely) the case!
  - Incorrect choices lead to incorrect parses since the algorithm cannot perform any backtracking
- Alternate sequences may also lead to equally valid parses

# How do we get actual dependency labels?

- Parameterize **LeftArc** and **RightArc**
  - LeftArc(nsubj), RightArc(obj), etc.
- Of course, this makes the oracle's job more difficult (much larger set of operators from which to choose!)

```
iobj(book → me)
compound(flight → morning)
det(flight → the)
obj(book → flight)
root(root → book)
```

# How does the oracle know what to choose?

- State of the art systems use **supervised machine learning** for this task
- This requires a training set of configurations labeled with correct transition operators
- The person designing the system needs to decide what types of features should be extracted from these configurations to best train the oracle (a machine learning model)
- The oracle will then learn which transitions to predict for previously-unseen configurations based on the extracted features and associated labels for configurations in the training set



# What types of machine learning models are used as oracles?

## Commonly:

- Logistic regression
- Support vector machines

## Recently:

- Neural networks

## Graph-based Dependency Parsing

- Search through the space of possible trees for a given sentence, attempting to maximize some score
- This score is generally a function of the scores of individual subtrees within the overall tree
- **Edge-factored approaches** determine scores based on the scores of the edges that comprise the tree
  - $\text{overall\_score}(t) = \sum_{e \in t} \text{score}(e)$
  - Letting  $t$  be a tree for a given sentence, and  $e$  be its edges

# Why use graph-based methods for dependency parsing?

- Transition-based methods tend to have high accuracy on shorter dependency relations, but that accuracy declines as the distance between the two words increases
- This is largely due to the fact that transition-based methods are greedy ...they can be fooled by seemingly-optimal local solutions
- Graph-based methods score entire trees, thereby avoiding that issue

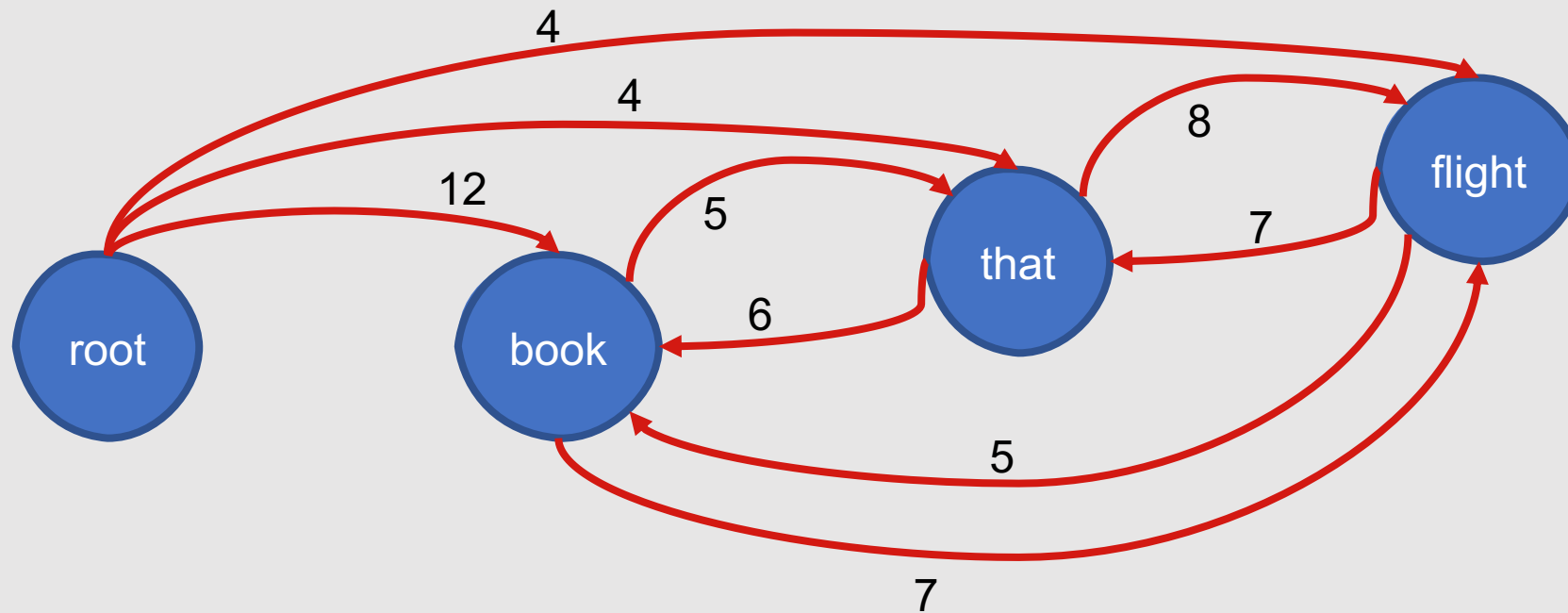
# Maximum Spanning Tree

Given an input sentence, construct a fully-connected, weighted, directed graph

- Vertices are input words
- Directed edges represent all possible head-dependent assignments
- Weights reflect the scores for each possible head-dependent assignment, predicted by a supervised machine learning model

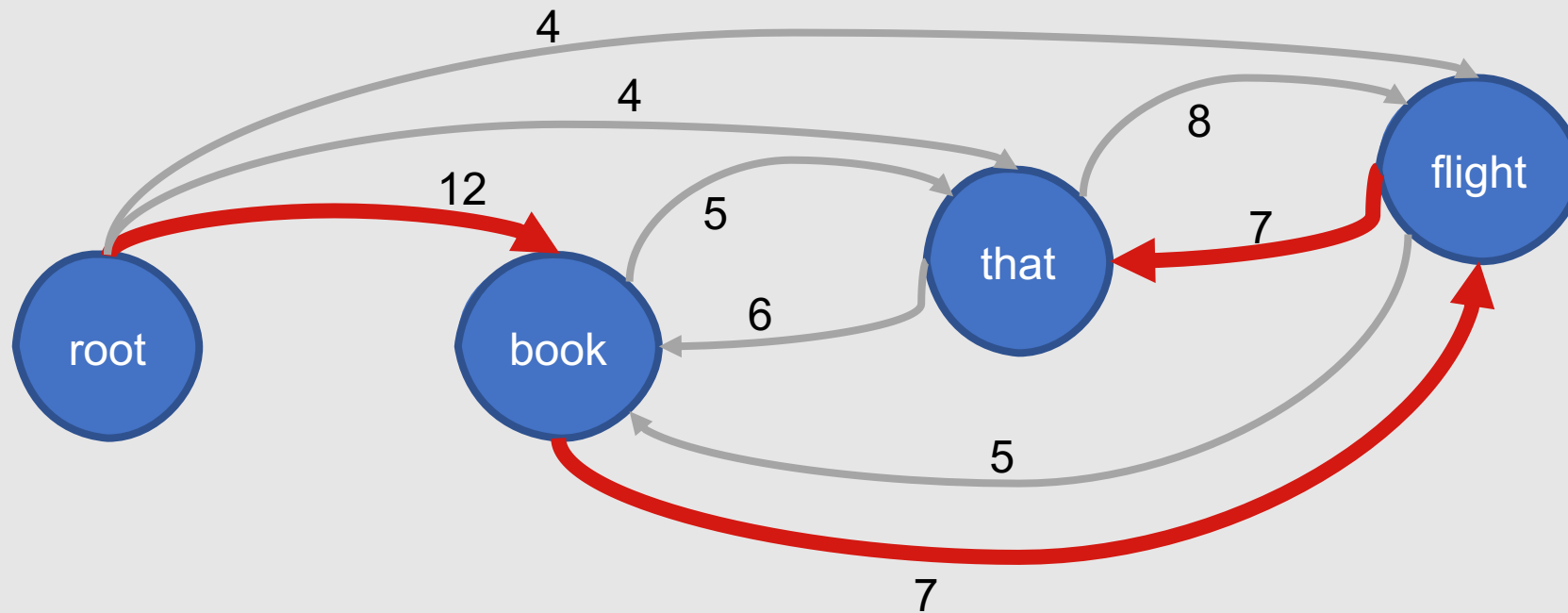
A maximum spanning tree represents the preferred dependency parse for the sentence, as determined by the weights

# Maximum Spanning Tree: Example





# Maximum Spanning Tree: Example



# Two intuitions to keep in mind....

- Every vertex in a spanning tree has exactly one incoming edge
- Absolute values of the edge scores are not critical
  - Relative weights of the edges entering a vertex are what matter!

How do we know  
that we have a  
spanning tree?

- Given a fully-connected graph  $G = (V, E)$ , a subgraph  $T = (V, F)$  is a spanning tree if:
  - It has no cycles
  - Each vertex (except the root) has exactly one edge entering it

# How do we know that we have a maximum spanning tree?

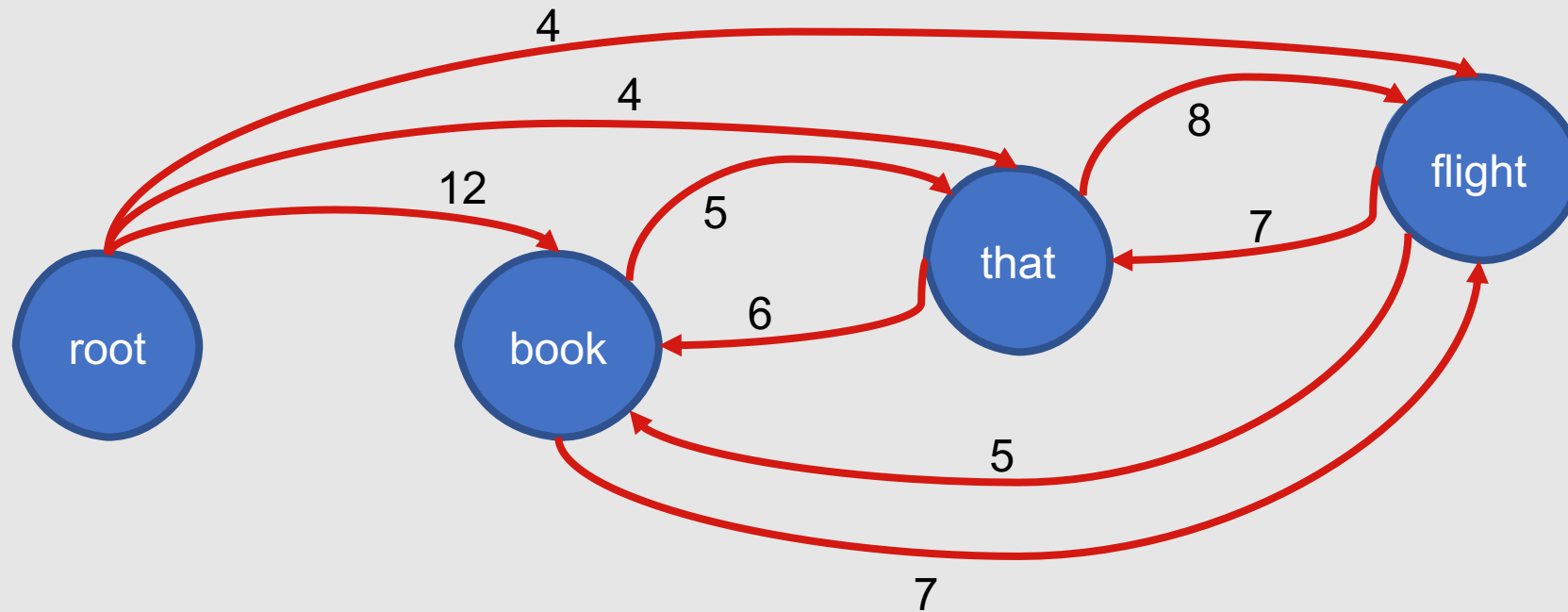
- **If the greedy selection process produces a spanning tree, then that tree is the maximum spanning tree**
- However, the greedy selection process may select edges that result in cycles
- If this happens, an alternate graph can be created that collapses cycles into new nodes, with edges that previously entered or exited the cycle now entering or exiting the new node
- The greedy selection process is then recursively applied to the new graph until a (maximum) spanning tree is found

# Formal Algorithm

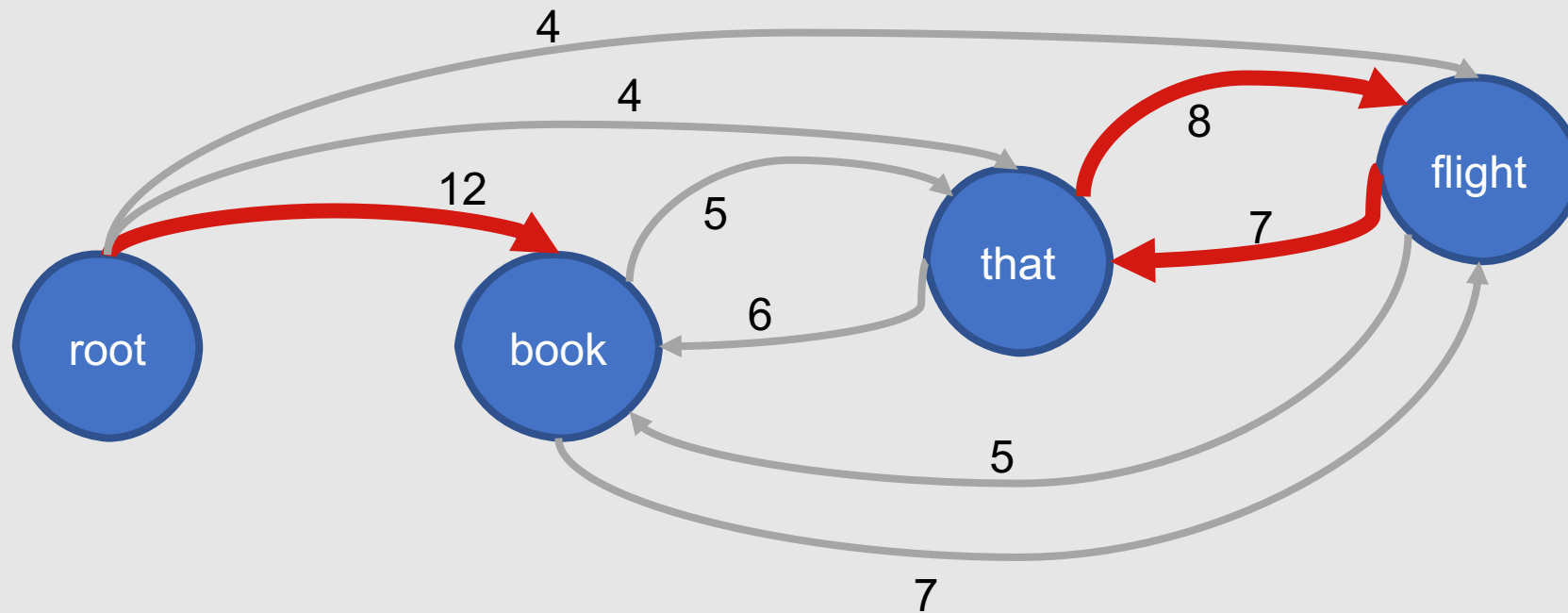
```
F ← []
T ← []
score' ← []
for each v in V do:
    bestInEdge ← argmaxe=(u,v)∈E score[e]
    F ← F ∪ bestInEdge
    for each e = (u,v) ∈ E do:
        score'[e] ← score[e] - score[bestInEdge]

    if T=(V,F) is a spanning tree:
        return T
    else:
        C ← a cycle in F
        G' ← collapse(G, C)
        T' ← maxspanningtree(G', root, score') # Recursively call the current function
        T ← expand(T', C)
        return T
```

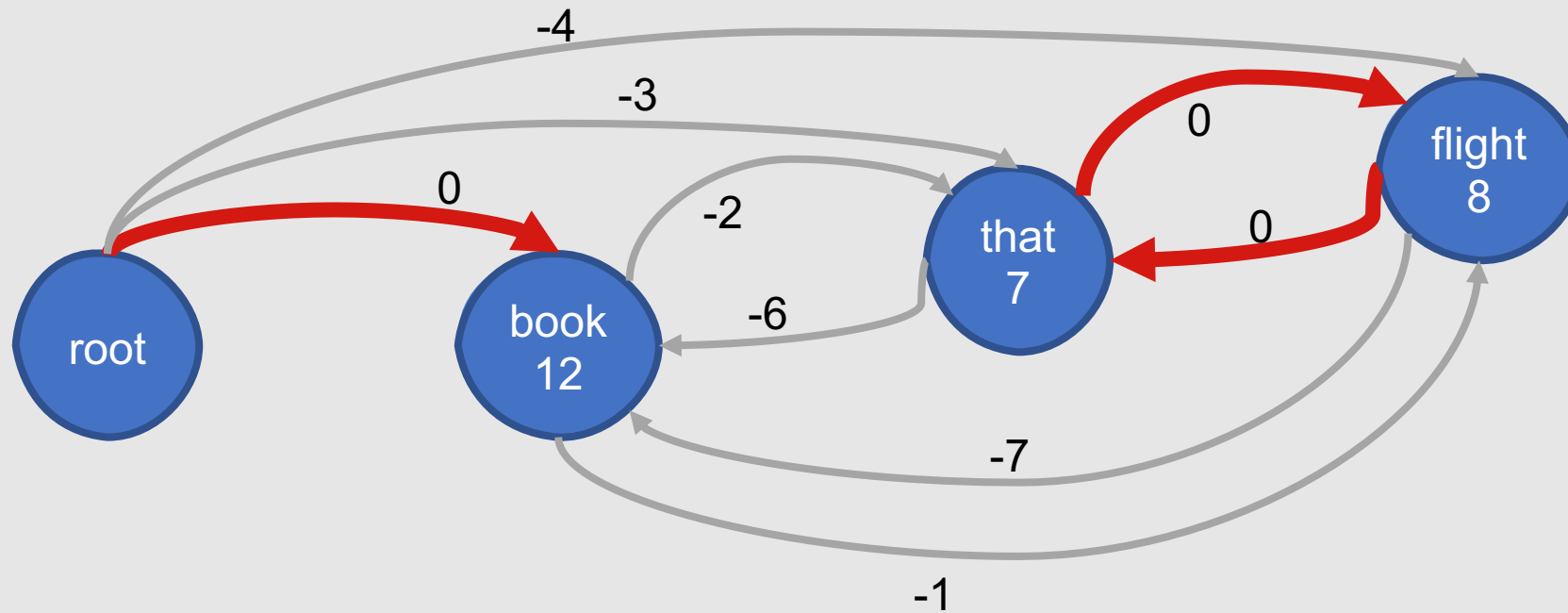
# Maximum Spanning Tree: Updated Example



# Maximum Spanning Tree: Updated Example

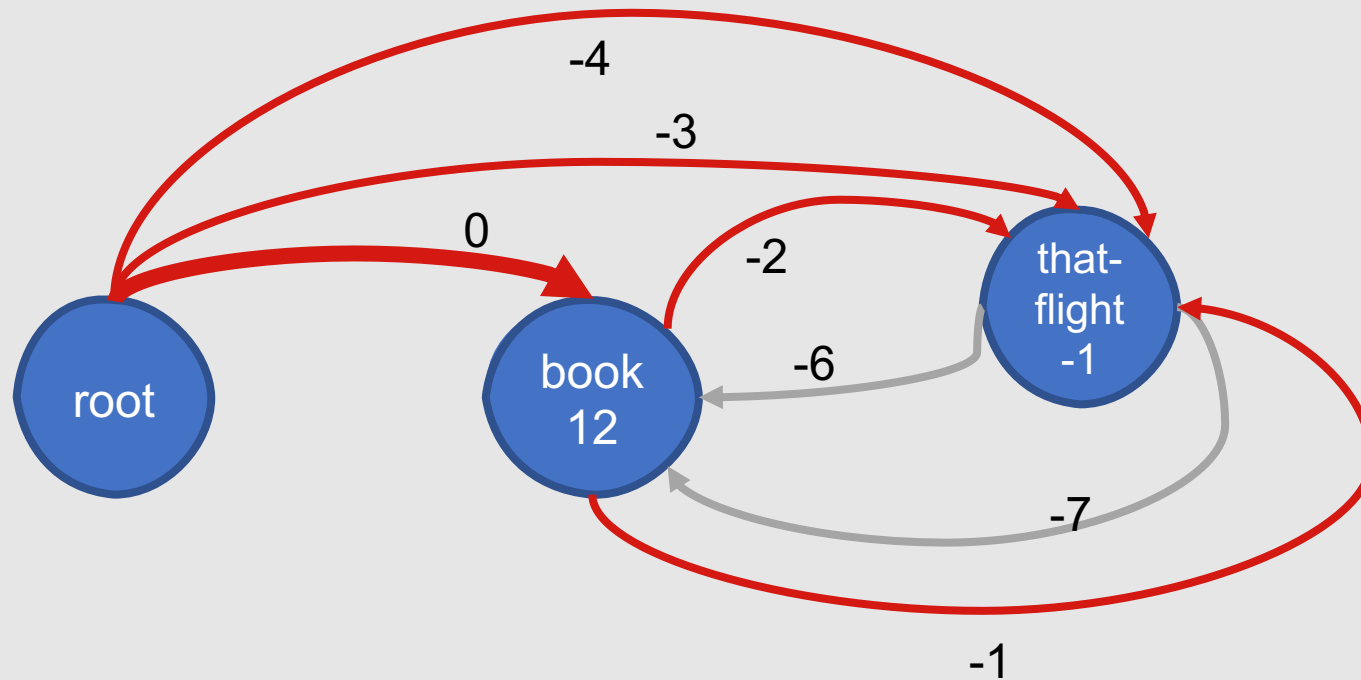


# Maximum Spanning Tree: Updated Example

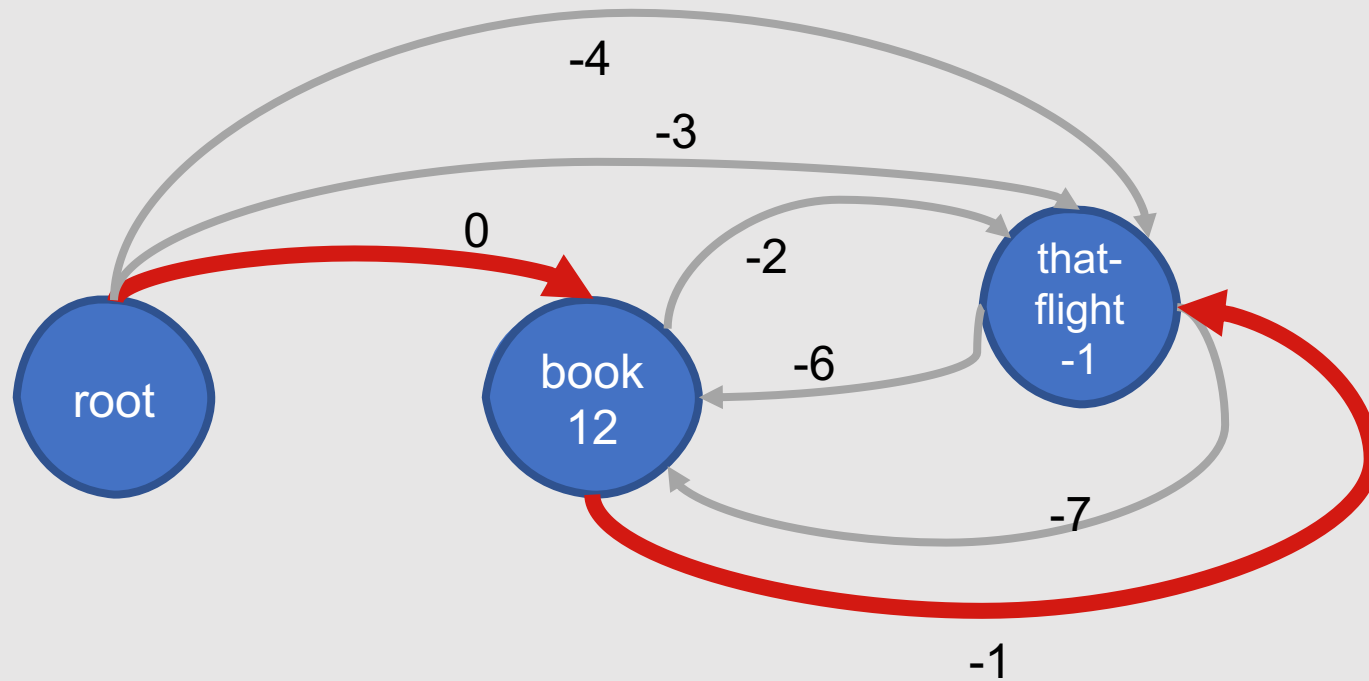




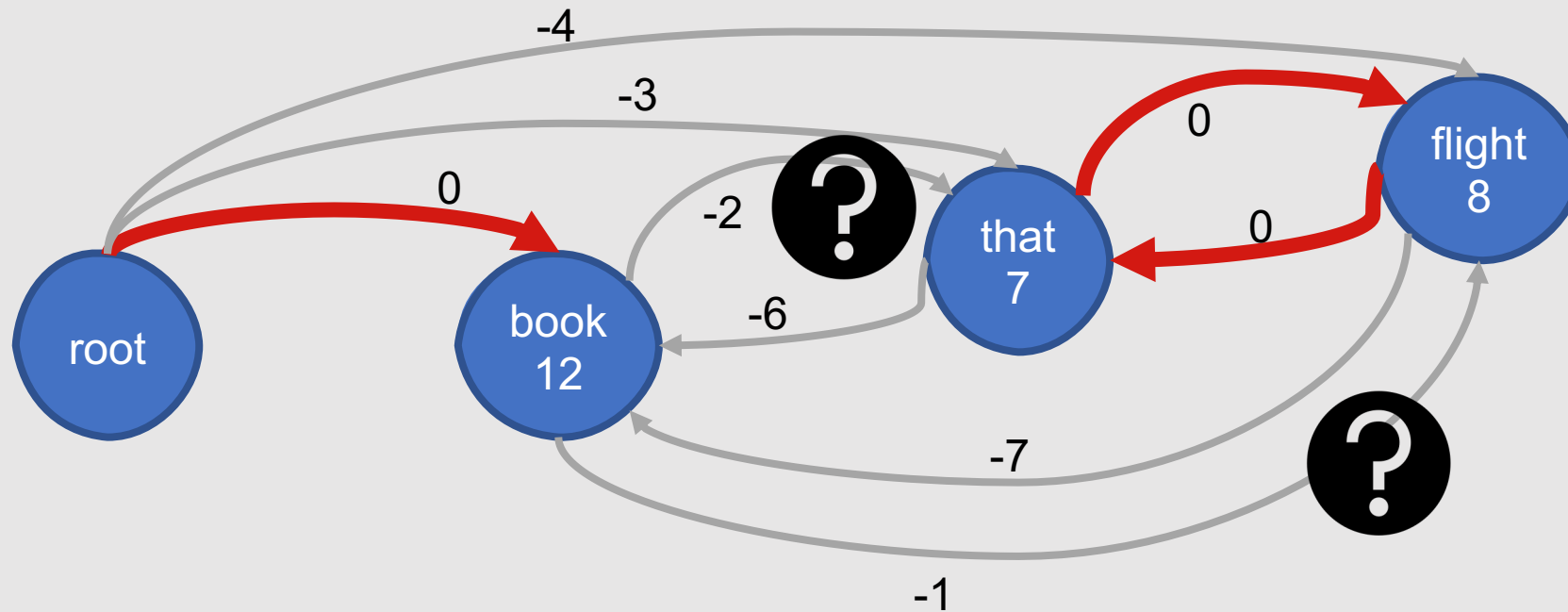
# Maximum Spanning Tree: Updated Example



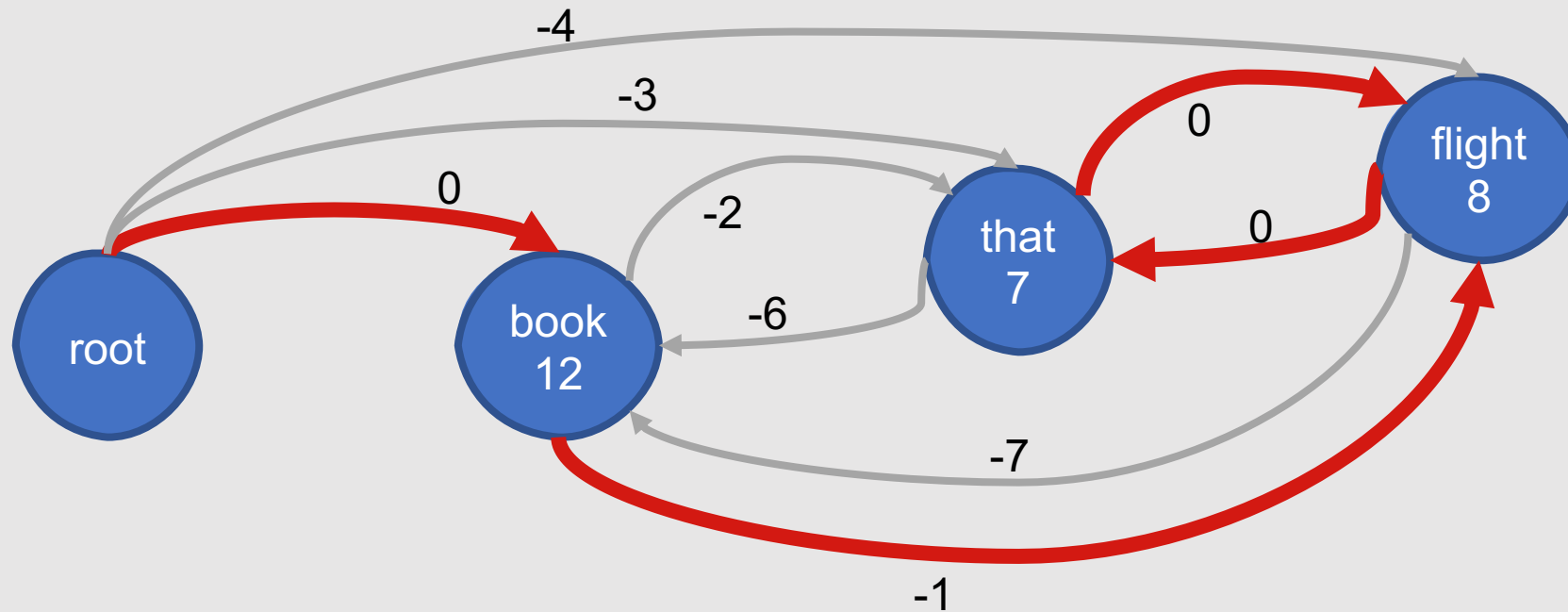
# Maximum Spanning Tree: Updated Example



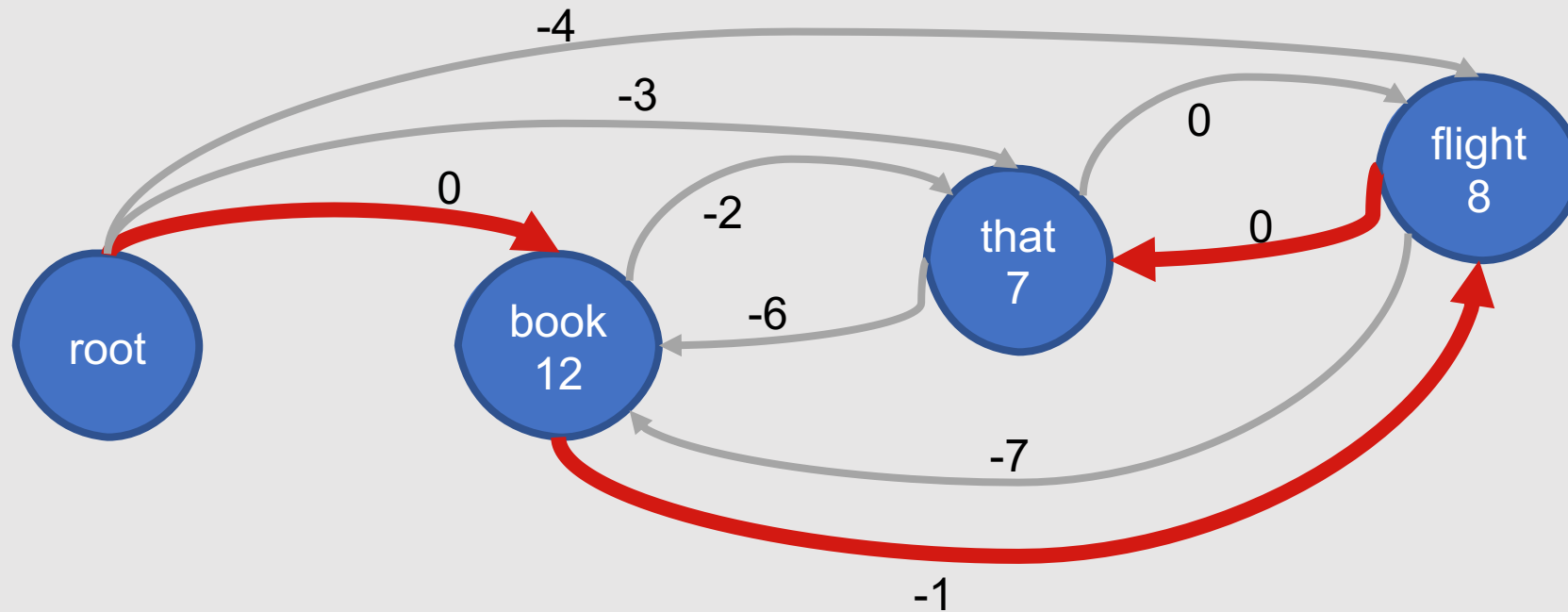
# Maximum Spanning Tree: Updated Example



# Maximum Spanning Tree: Updated Example



# Maximum Spanning Tree: Updated Example



# How do we train our model to predict edge weights?

- Similar approach to training the oracle in a transition-based parser
- Common features can include:
  - Words, lemmas, parts of speech
  - Corresponding features from contexts before and after words
  - Word embeddings
  - Dependency relation type
  - Dependency relation direction
  - Distance from head to dependent

# Summary: Dependency Parsing

- **Dependency parsing** is the process of automatically determining **directed relationships between words** in a source sentence
- Many dependency taxonomies exist, but the most common taxonomy for English text is the set of **universal dependencies**
- Dependency parsers can be **transition-based** or **graph-based**
- A popular transition-based method is the **arc standard** approach
- A popular graph-based method is the **maximum spanning tree** approach
- Both make use of **supervised machine learning** to aid the decision-making process